

Klima 2.0

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An **Autonomous Asset Manager** incorporating asset pricing, liquidity and time-locked markets powered by a dual token structure designed for efficient and rational decentralised liquidity within the carbon credit asset class.



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1 Prologue

Klima 2.0 is an autonomous capital system for the carbon asset class. It is neither a conventional token nor a traditional protocol, but rather a continuously adaptive financial structure governed entirely by endogenous signals and risk-weighted economic inputs.

The system is based on a dual token architecture: **kVCM**, representing capital and asset exposure, and **K2**, reflecting systemic risk preferences. Together, these tokens structure the internal market dynamics without the need for oracles or discretionary oversight. This architecture enables the system to:

- Systematically select and price tokenised carbon credits,
- Construct and maintain a forward-yield curve derived from on-chain capital commitments,
- Govern portfolio allocation, liquidity provisioning, and incentive distribution through deterministic smart contract logic.

All token holder actions – locking, allocation and staking – serve as inputs to a reflexive coordination mechanism. **kVCM** governs the allocation of capital to carbon assets, while **K2** parametrises the system’s risk assumptions and pricing capacity. This interaction defines a synthetic balance sheet where capital value, risk spread, and yield formation emerge from collective participation.

The platform consists of three interdependent components: the **Portfolio Manager**, which acquires and retires carbon assets; the **Time-Locked Market**, which generates a time-structured synthetic yield curve; and the **Liquidity Market**, which facilitates price discovery and capital flow across **kVCM**, **K2**, and external currencies. These mechanisms are interlocked by design, enabling the system to continuously seek equilibrium.

Klima 2.0 abstracts complex market operations into a formal economic structure that integrates asset management, governance, and liquidity within a single protocol. **kVCM** offers structured exposure to carbon markets through tokenised yield and asset ownership, while **K2** modulates this exposure in response to endogenous risk metrics.

In this model, staking constitutes an economic vote; liquidity provision informs portfolio capacity; and yield is an emergent function of structural configuration. The system is designed to operate without exogenous intervention, maintaining equilibrium through adaptive incentive distribution and real asset correlation.

Klima 2.0 is a closed-form capital system with embedded governance and economic reflexivity, capable of continuously modelling and adjusting its internal state through its own token dynamics.

2 Klima 2.0

KlimaDAO launched in 2021 on the Polygon blockchain as a fork of OlympusDAO. The original system centred on the KLIMA token backed by a treasury of carbon credits. At its peak, the KLIMA token exceeded a one-billion-USD market cap and brought over 20 million tonnes of carbon credits on-chain through incentives and governance.

Supporters agree that voluntary carbon markets benefit greatly from tokenisation and on-chain liquidity. This brings transparency, price discovery, accessibility, interoperability, programmability, and faster settlement for brokers and buyers. These benefits are proven by dozens of production-grade platforms and services built by Klima and partners after launch, including:

- Integrations with major carbon registries.
- Marketplaces, storefronts, and point-of-sale tools.
- REST APIs for seamless integration into third-party apps.
- Direct blockchain issuance by major project developers.

All of these products are powered on KlimaDAO’s tokenised carbon and liquidity, with measurable adoption. This makes the KLIMA token a leading case study for the adoption of tokenised Real World Assets.

Still, after years of iteration it became clear that Klima 1.0 and the KLIMA token would not be able to scale or serve the largest enterprise buyers effectively.

Hence we present **Klima 2.0** as an **Autonomous Asset Manager** (AAM) with the new **Risk-Balanced Asset** token **kVCM** that:

- Selects and purchases carbon credits on a spot and forward basis for its own portfolio.

- Retires its carbon credits by issuing carbon offset certificates to buyers.
- Continuously yields carbon credits from its portfolio.
- Enables investors to:
 - Hold a true *passive* exposure to carbon markets, spreads and dislocations via the new **kVCM** token.
 - *Actively* reflect their risk appetite collectively to optimise portfolio selection and capacity.
 - Determine the proportion of yield distribution vs capital retention, allowing cyclical expansions and contractions and de-facto price modelling of the **kVCM** token.

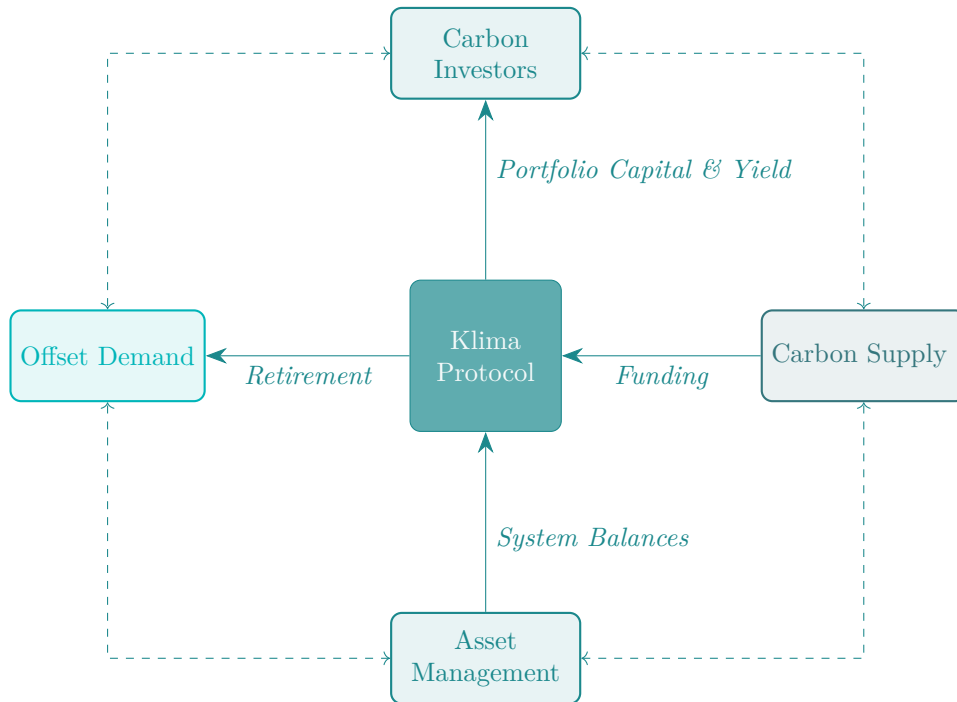


Figure 1: Klima 2.0 high-level design.

Klima 2.0 provides a fundamental capital, liquidity and execution layer for wholesale carbon trading, capturing spreads and structural pricing across the asset class. It employs rational adaptive financial models to reflect token holders' collective risk-reward preferences, produced solely through native smart contract balances from staking and liquidity functions allowing price discovery and harmonious functions to govern the stability and risk of the Risk-Balanced Asset token **kVCM**.

The model grants clean *look-through* economic ownership of tokenised carbon assets to **kVCM** token holders, as well as self-governance for risk and reward allowing maximum flexibility in this hybrid capital instrument for growth and distribution.

2.1 Dual Utility Tokens

In addition to the **kVCM** token, Klima 2.0 introduces a second **Risk Governance** token **K2**. This token is responsible for modelling risk across the ecosystem by responding to the **kVCM** token's core selections and adding essential derivative parameters that manage adverse selection and pricing capacity.

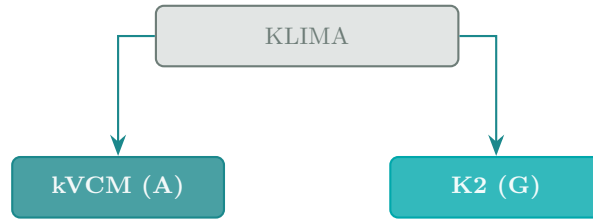


Figure 2: Token replacement.

kVCM tokens have the beneficial ownership of the portfolio and set core allocation choices, whereas **K2** acts as the *risk-seeking* gauge for the portfolio construction.

K2 is formally compensated with **kVCM** tokens hence the two tokens' interests are fully aligned, and together perform dynamic portfolio optimisation as a result of collective owner utility function.

2.2 High-Level Architecture

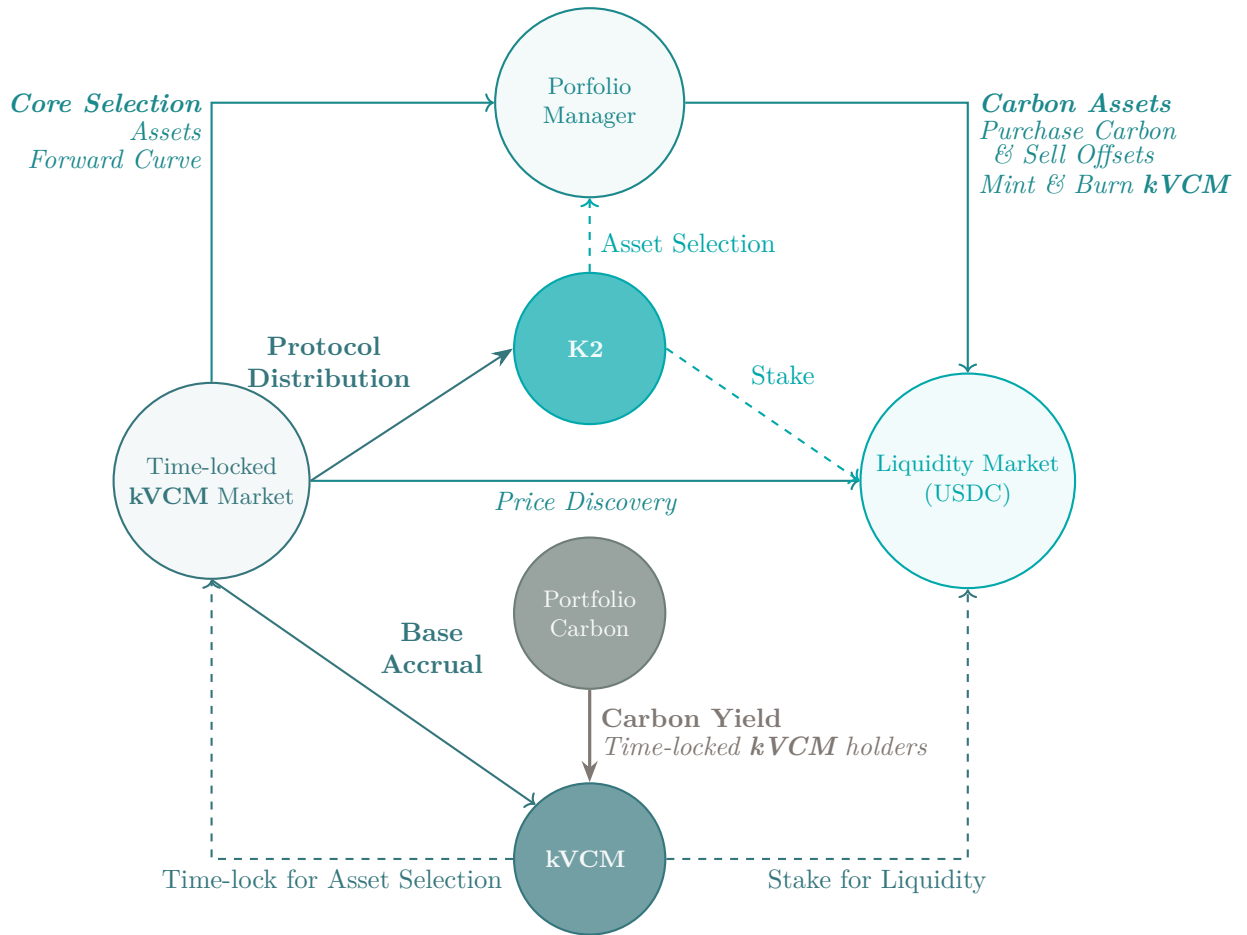


Figure 3: Klima 2.0 architecture.

Three economic pillars support the Klima 2.0 Automated Asset Manager:

1. Portfolio Manager:

- Accumulates carbon credits for the portfolio by minting **kVCM**.
- Sells carbon offset certificates from the portfolio by burning **kVCM**.
- Prices **liquid carbon** ('spot' or 'ex-post credits') and **forward-delivery carbon** ('ex-ante credits') using the system's generated discount rates.

2. Time-Locked Market:

- **kVCM** holders **time-lock** their **kVCM** irreversibly for a fixed time period.
- Time-locked **kVCM** holders are able to *select* carbon assets for the portfolio.
- The time-locking pattern creates a **kVCM** Base Accrual curve, which is distributed to time-locked **kVCM** holders. This is utilised to derive discount rates for forward-delivery pricing in the Portfolio Manager and for weightings for time-locked **kVCM** holders in governance, as well as for their liquid carbon distribution.

3. Liquidity Market:

- **kVCM** and **K2** holders are able to pair their tokens together, or in the case of **kVCM** with USDC, in order to generate liquidity fees.
- Staking the resulting liquidity provider tokens generates a share of the **kVCM** risk premium.
- Liquidity locked in the **kVCM/K2** liquidity pool participates in general governance alongside time-locked **kVCM** holders.

Noting that throughout the paper, *locking* and *staking* mean that asset transfers are disabled for a specified period.

2.3 Economics and Incentives

2.3.1 kVCM Synthetic Yield

kVCM emits a continuous yield rewarding:

1. Time-locked **kVCM** holders ('**kVCM** Base Accrual').
2. User-locked **K2** holders ('**kVCM** Risk Premium').
3. Both **kVCM** and **K2** stakers, i.e. liquidity providers who staked their liquidity provider tokens ('**kVCM** Risk Premium').

The proportions and quantities are dynamic depending on the system state.

2.3.2 K2 Incentives

The expansion of the **K2** token supply is allocated to stakeholders below in varying quantities depending on system balances.

1. Time-locked **kVCM** holders.
2. User-locked **K2** holders.
3. Both **kVCM** and **K2** stakers.

2.3.3 Real Carbon Yield

Assuming the portfolio holds liquid (spot) carbon credits, the Portfolio Manager emits a continuous Liquid Carbon Yield to time-locked **kVCM** holders with the proportion a function of the system state.

2.4 Portfolio Manager

At the core of the platform, the Portfolio Manager accumulates, trades and distributes its carbon portfolio driven by parameters determined from collective token holder actions (and inaction).

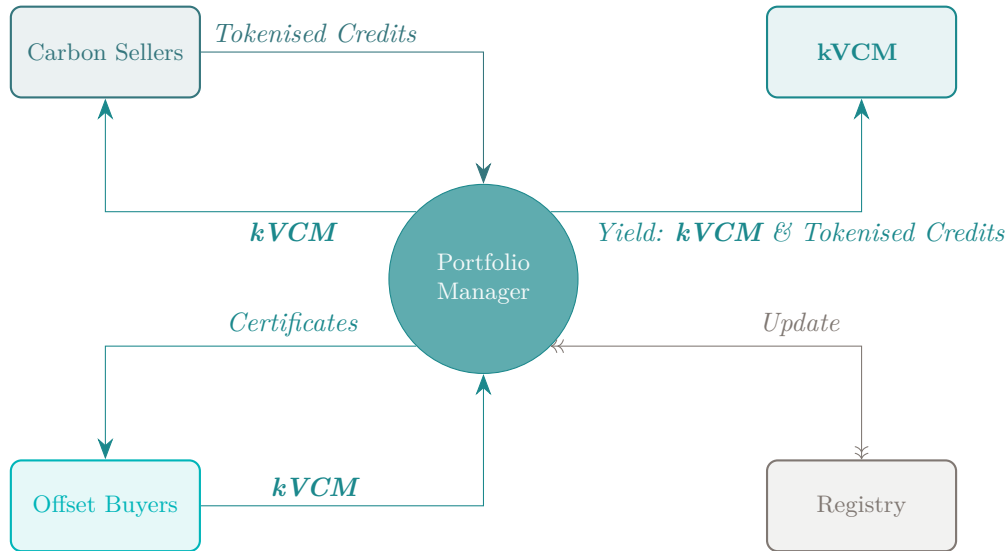


Figure 4: Klima 2.0 Portfolio Manager.

The Portfolio Manager **purchases** carbon credits and **sells** offset certificates by pre-defined classification called **carbon class**. It does not sell carbon credits as those are issued through the Liquid Carbon Yield function.

Token holders collectively set the risk parameters for the pricing of **each class** by defining:

- Portfolio weighting.
- Capacity curve and spreads.

Additional **global** parameters are similarly determined:

- Forward-delivery discount rates.
- **kVCM** synthetic yield curve creating incentives for portfolio selection, liquidity provision and risk management contributions.
- Proportion of Liquid Carbon Yield released for time-locked **kVCM** holders.

There are no oracles or external inputs required for Klima 2.0 as it is fully autonomous and responds to its own native state of token balances.

2.5 Tokens

2.5.1 Risk-Balanced Asset Token: **kVCM**

kVCM represents core ownership of the portfolio assets, and is designed to flex between asset and growth value drivers depending on token-holder activity.

kVCM has no maximum supply but inflates upon carbon credit accumulation, and contracts upon issuance of carbon offset certificates.

- When **time-locked** for fixed maturities:
 - *Optionally* selects carbon classes for portfolio weighting and pricing ('active').
 - Sets the forward discount rate for carbon portfolio acquisition from the collective time locking pattern over time.
 - Generates a **synthetic yield** of **kVCM** based on the forward curve and a **Liquid Carbon Yield** based on the active selection ratio.
 - Participates in governance for whitelisting carbon assets.
- **Transactional** usage:
 - **Mint**: New **kVCM** is issued by the Portfolio Manager to purchase new carbon credits for the portfolio.
 - **Burn**: **kVCM** are retired by the Portfolio Manager to issue carbon offset certificates.
- **Staked** liquidity:
 - Generates a **kVCM** Risk Premium, which is a time-based relative share of the **kVCM** synthetic yield reflecting the risks taken to support the price of platform capital.

Noting that the tokens can delegate utility as required.

2.5.2 Risk Governance Token: **K2**

K2 is a fixed-supply token issued programmatically over time with a dynamic allocation for **K2 Incentives**.

- When **user-locked**:
 - Shapes the pricing curve and spread of **kVCM**.
 - Determines the **kVCM** Risk Premium for staked liquidity providers.
 - Generates a share of the **kVCM** Risk Premium.
 - Receives **K2** Incentives.
- **Staked** Liquidity:
 - Generates a share of the **kVCM** Risk Premium.
 - Participates in governance.
 - Receives **K2** Incentives.

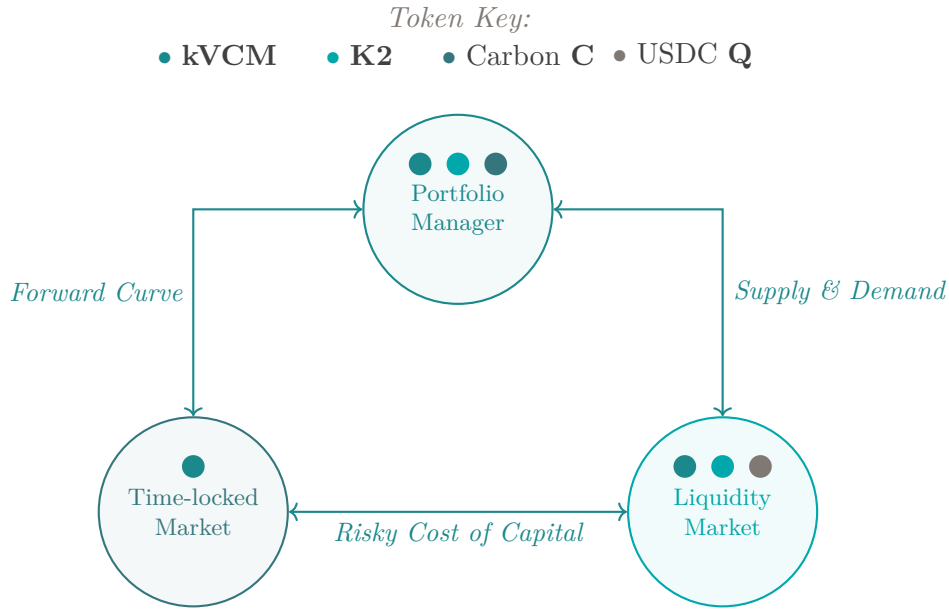


Figure 5: Automated Asset Manager token utility.

2.5.3 Utility Functions

The **kVCM** token has two utility functions which are not independent:

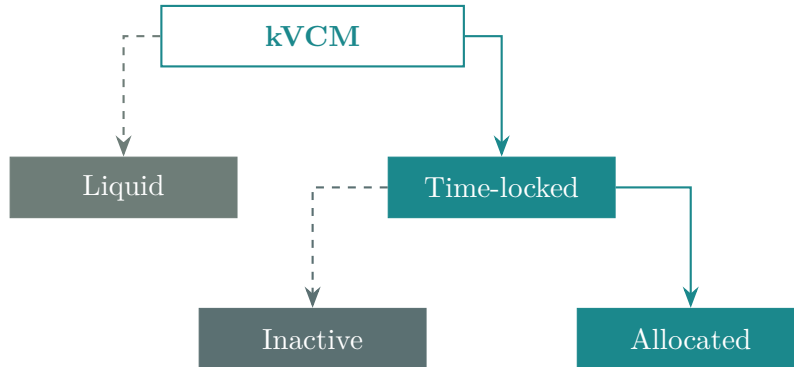


Figure 6: **kVCM** utility functions.

1. **Time lock:** The **kVCM** token is locked for a specific period of time representing a liquidity preference for the holder in return for yield ('**kVCM** base accrual'). This cannot be amended.
2. **Price allocation:** Collective selection of carbon classes by **kVCM** allocations determines the **instantaneous** price ratio for **kVCM** token issuance. This selection can be amended and withdrawn at any time to allow price modulation for the platform of its carbon assets.

The **K2** token also has two utility functions:

1. **User lock:** The **K2** token remains locked for at least 24 hours.
2. **Risk allocation:** collective selection of carbon classes by **K2** allocations determines the rate of issuance or price curve of **kVCM** for the specified carbon class, as well as the retirement burning rate.

Both tokens facilitate the carbon market to function efficiently with the **kVCM** token responsible for portfolio selection and pricing, and the **K2** token modulating capacity and risk.

2.6 Initialisation of the kVCM Token

The Klima Protocol has approximately **20 million tonnes** of carbon credits in its treasury as assets, a part of which will be used to create the initial issuance of **kVCM** tokens upon launch of Klima 2.0.

Token	Amount	Notes
kVCM A Token	20 million	• Supply expands and contracts perpetually. • 87.5% of initial supply available to existing KLIMA holders. • Initially created approximately on a 1:1 basis with carbon tonnes held.
K2 G Token	100 million	• Issues on carbon received, and burns on carbon retired. • Fixed supply. • 40% put into programmatic issuance as K2 Incentives yield over time. • 40% for existing KLIMA holders.

Table 1: Token Summary

2.7 End Users

1. Carbon Credit Sellers

Those wishing to monetise spot- or forward-delivery classes of carbon.

***Portfolio Manager:** Continuously acquires carbon credits using an autonomous pricing strategy based on carbon class, delivery and token balances, issuing new **kVCM** tokens as consideration to build the carbon portfolio.*

2. Offset Buyers

Those wishing to obtain carbon offset certificates by retiring carbon credits from the portfolio.

***Portfolio Manager:** Continuously sells carbon offset certificates, by burning **kVCM** tokens and issuing carbon offset certificates by retiring the quantity in the registry.*

3. Investors

Those who wish to own a liquid or yielding locked fixed-maturity financial exposure to a basket of carbon assets.

***Time-Locked Market:** Provides a daily time-based yield for those time-locking **kVCM** tokens, comprised of both a synthetic **kVCM** Base Accrual and real portfolio Liquid Carbon Yield component.*

4. Liquidity Providers

Those who wish to generate liquidity fees on their portfolio of Klima 2.0 assets coupled together or with USDC.

***Liquidity Market:** Staked liquidity providers are incentivised by the **kVCM** Risk Premium calculated from system metrics to compensate them for risk.*

5. Active Portfolio Optimisation

***K2 and kVCM Asset Selection:** The incentives and allocations are designed for those who wish to participate in overall risk management to collectively resolve for the optimal portfolio risks.*

2.8 Automated Asset Manager Highlights

- **Decentralised architecture:**

The Automated Asset Manager is smart-contract based, fully autonomous as to pricing and distribution of its assets with governance power held by risk-based capital.

- **Adverse selection:**

The Automated Asset Manager does not permit the direct purchase of carbon credits from its portfolio (only carbon offset certificates), but rather yields liquid carbon on a portfolio basis over time.

- **Liquid carbon:**

Users with liquid carbon credits can always access carbon offset certificates through the registry, hold the specific carbon credits or sell back to the Automated Asset Manager if required. Secondary markets and utility for liquid carbon credits may emerge over time.

- **Implied spreads:**

The Automated Asset Manager purchases carbon at relative discounts based on capacity pricing and forward discount rates folding natural returns into the portfolio capital.

- **Dual token structure:**

Whilst the **kVCM** token reflects asset economics, the **K2** token is essential for optimising pricing capacity and in return **maximising risk-adjusted spreads** for the portfolio. Since its earnings power is a function of the **kVCM** token value, its role as this spread optimiser is truly economically aligned and as such fundamental values of **kVCM** and **K2** are highly correlated.

- **Hybrid asset model**

The rate of Liquid Carbon Yield for **kVCM** generated from the underlying portfolio is derived from the system state of the **kVCM** token balances.

- This enables investors collectively to model capital and yield proportions, allowing the price of the capital token to discover its **equilibrium** value with respect to the combination of **current** and **projected** underlying portfolio value.
- This flexibility enables a ‘pull to par’ effect as growth expectations lower, whilst not limiting price appreciation potential in high growth projection markets.
- The hybrid model incorporates both **asset stabilisation** plus **equity-like** returns.

Critically this approach enables the **kVCM** token to act as a true medium of exchange for the carbon trading activity of the users, propagating the feedback loops to both the **kVCM** and **K2** tokens.

3 Core Economic Pillars

From this Section, we refer to **kVCM** and **K2** tokens as **A** and **G** respectively.

The three tenets of Klima 2.0 enable the model to find equilibrium through continuous dynamic feedback loops and system balances. There is no oversight or centralised management entity with discretionary powers.

1. **Time-Locked Market:** **A** token holders stake tokens until a set expiry to create floating yield time locks and have the ability to select carbon classes for portfolio weighting.
 - The collective temporal staking pattern produces a **Synthetic Yield** curve in **A** tokens to reward time-locked token holders, as well as price the forward curve for the AAM.
 - A **Liquid Carbon Yield** is issued continuously from the portfolio to time-locked **A** holders depending on the participation in portfolio weightings.
 - Only **A** tokens participate in the Time-Locked Market.
2. **Portfolio Manager:** The Portfolio Manager swaps its own token **A** for carbon credits **C** (in) or carbon offset certificates **C*** (out) to build a portfolio of carbon credits.
 - Both **time-locked A** and **user-locked G** are used in the portfolio manager whereby allocating **A** determines the pricing of any given carbon class, and allocating **G** determines the rate of acquisition (and disposal).

Only time-locked A tokens can participate in portfolio weighting although it is not mandatory.

 - Forward-delivery carbon (for a set of fixed dates out to 10 years) is transacted simultaneously with spot liquid carbon.
3. **Liquidity Market:** Here the tokens are traded in two core liquidity pairs with various incentives available to staked liquidity providers (**LPs**), including a **Risk Premium** generated by the Time-Locked Market synthetic yield.
 - $\overline{AG}$: Native token swap **A** and **G**.
 - $\overline{AQ}$: The asset token **A** with USDC **Q**.

The Liquidity Market provides the complementary facility to the Time-Locked Market and the critical relationship between the native tokens and the hard currency of USDC.

The Klima 2.0 system enables each participant in the various economic pillars to act in the interests of their own capital and utility, which through the harmonic model, enables price discovery, liquidity and stability for carbon trading which creates positive reinforcement cycles as catalysts for growth and scale.

3.1 Time-Locked Market

Holders of **A** can time-lock their token until a maturity from the set of **standard maturities**. Time locks expire every 90 days on a rolling basis. There are always 40 maturities extending out to approximately 10 years.

- **Forward curve:** Aggregate time-locking determines the shape of the discount curve of the **A** token with regards to its purchasing rate of forward-delivery carbon.
- **Synthetic yield:** Time-locked **A** token holders receive a floating yield of new **A** tokens following the shape of this discount curve called **Base Accrual**. Base Accrual is calculated daily and accumulates to the principal.
- **Liquid Carbon Yield:** Liquid Carbon emitted to time-locked **A** token holders on a daily basis assuming the portfolio holds liquid carbon assets. The emission rate responds to time-locked **A** token holders allocating their token for portfolio pricing, and up to ~22% per quarter is released.
- **Liquidity:** There is no early unlocking; all principal and accumulated yield is released only at time lock expiration.

G tokens are not involved in the Time-Locked Market. The forward curve is agnostic to carbon class although only time-locked **A** token holders can allocate their token to carbon classes for portfolio pricing.

3.1.1 Synthetic Yield and Forward-Delivery Curve

Defining:

- S : Total time-locked **A** tokens expressed as a proportion of the outstanding supply of **A**.
- S_t : Total **A** tokens time-locked in maturity bucket t , expressed as a proportion of the outstanding supply of **A**, where $\sum S_t = S$, and t is the index of standard maturities $t \in \{1, 2, 3, \dots, 40\}$.
- E_t : Time to expiry expressed in years.

Calculating curve parameters D and C :

$$D = \frac{1}{S} \sum_{t=1}^{40} S_t E_t \quad (1)$$

$$C = \frac{1}{S} \sum_{t=1}^{40} S_t E_t^2 \quad (2)$$

The shape of the synthetic yield curve is produced:

$$\gamma_t = \max \left(\frac{E_t}{D} - \frac{E_t^2}{2C}, 0 \right) \quad (3)$$

Normalising γ_t to $\hat{\gamma}_t$:

$$\hat{\gamma}_t = \frac{\gamma_t}{\sum_{t=1}^{40} \gamma_t} \quad (4)$$

With the cumulative sum of the normalised values expressed as Γ_t :

$$\Gamma_t = \sum_{i=1}^t \hat{\gamma}_i \quad \text{for } t = 1, \dots, 40 \quad (5)$$

The zero-coupon yield curve Z_t is solved:

$$Z_t = (1 - S) \frac{\Gamma_t}{E_t} \quad (6)$$

Whereupon, the discount rate B_t that forms the forward-delivery curve is derived:

$$B_t = \exp(-Z_t E_t) \quad (7)$$

The yield due on time-locked **A** tokens is calculated daily and added to the staked principal, hence the daily yield for each time bucket is calculated:

$$Y_t = \exp\left(\frac{Z_t}{365}\right) - 1 \quad (8)$$

Hence, any time-locked **A** stake S_t will increase by ΔS_t :

$$\Delta S_t = S_t Y_t \quad (9)$$

With the total **A** tokens created on a daily basis for time-locked inflation as

$$R = \sum_{t=1}^{40} \Delta S_t \quad (10)$$

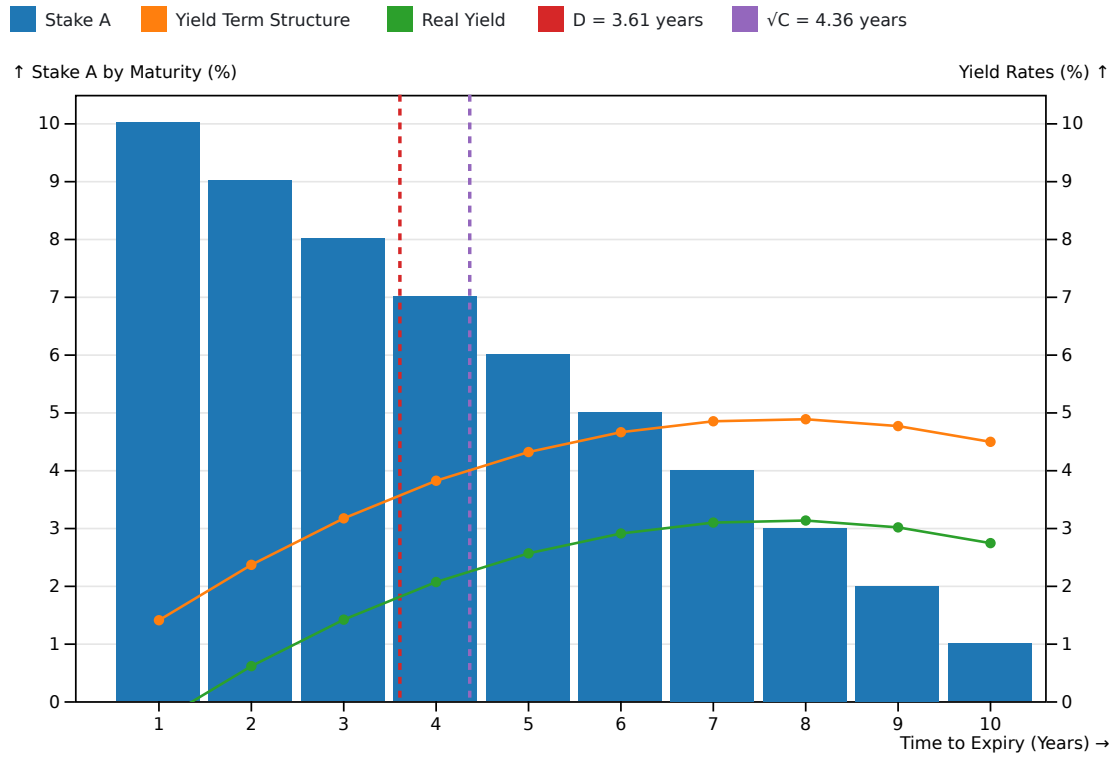
For visualising the sensitivity of overall **A** inflation rates with respect to staking and duration, Figure 8 assumes a single maturity over the staking range to provide an approximation of inflation $\Delta S \approx Z S$.

3.1.2 Governance Weightings

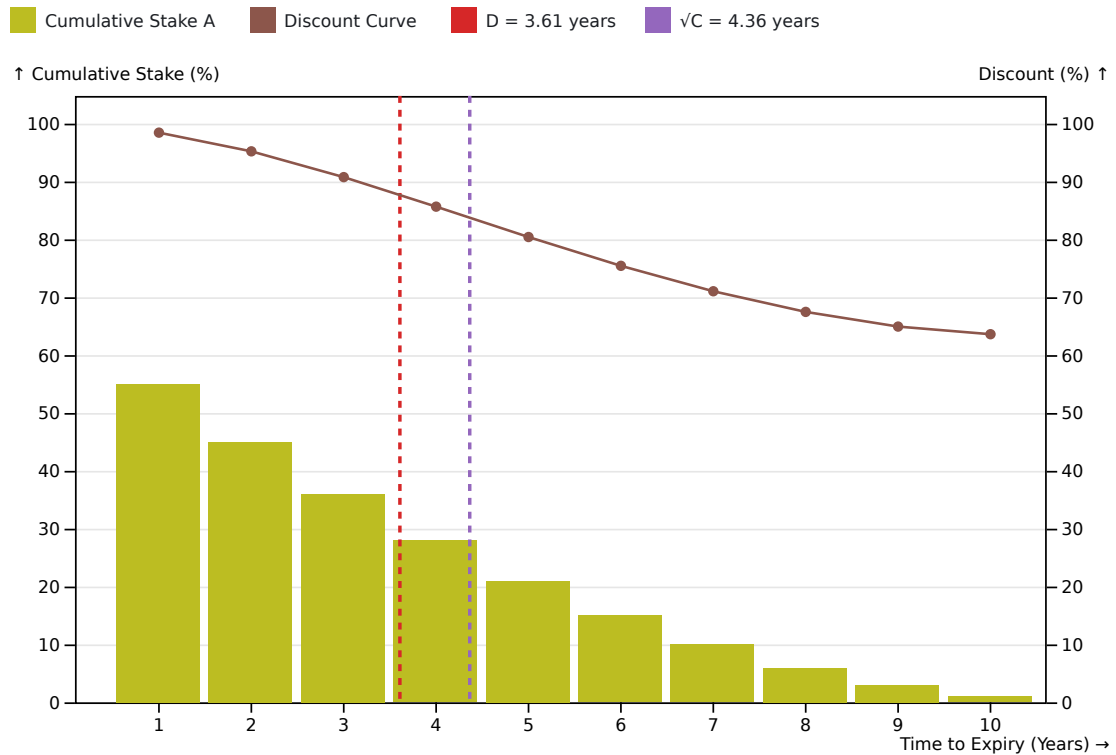
Governance rights, for example the whitelisting (and blacklisting) of carbon classes, and any other matter requiring token stakeholder voting, are allocated to two cohorts:

1. Time-locked **A** tokens: S_t
2. Staked liquidity in the **A-G** pair $\overline{\mathbf{AG}}$ (see Section 3.3), defined here as A_{Gt} , representing the quantity of **A** tokens held in the liquidity pool expressed as a proportion of circulating supply.

Voting power is allocated by time and applied to the respective balance of **A**:



(a) Yield (Total Stake = 55.00%, Inflation = 1.75%).



(b) Discount rate.

Figure 7: Example of a Time-Locked Market state.

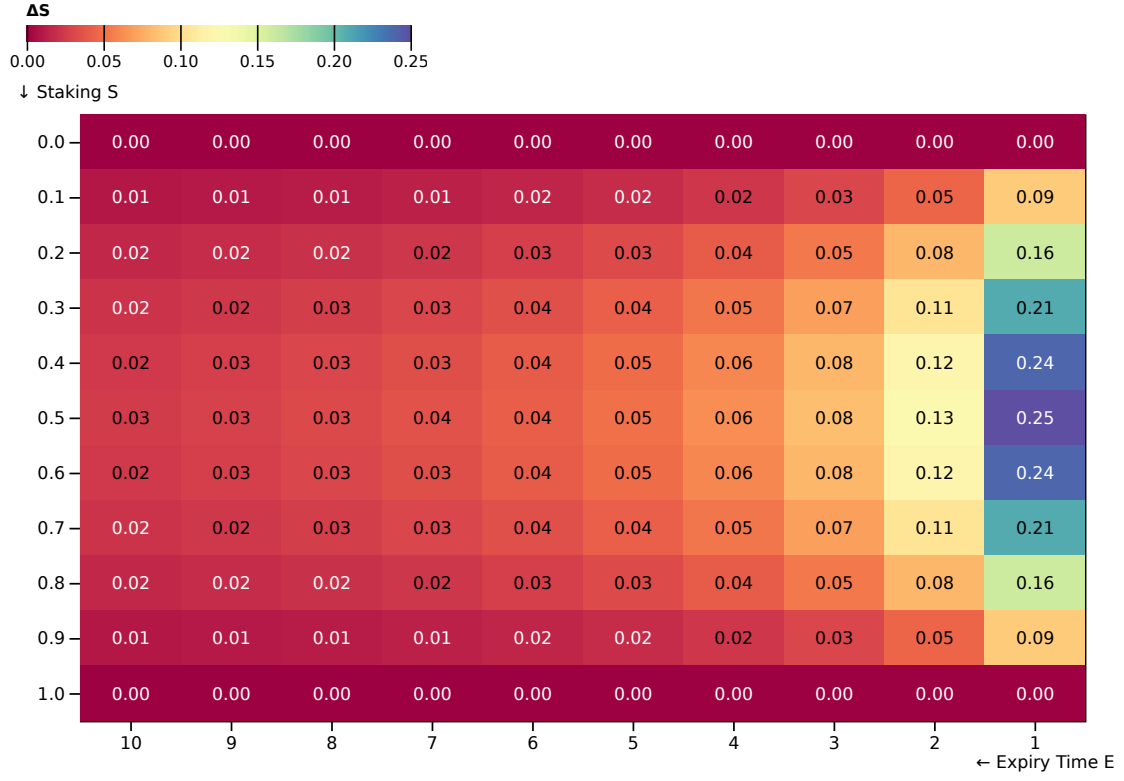


Figure 8: **A** inflation rate from time-locked token yields ΔS .

1. Initial voting weights for time-locked **A** tokens v_t :

$$v_t = Z_t S_t \quad (11)$$

2. Initial voting weights for staked liquidity w_t :

$$w_t = Z_t A_{Gt} \quad (12)$$

3. Final voting weights for time-locked **A** tokens V_t :

$$V_t = \frac{v_t}{\sum_{j=1}^{40} (v_j + 2w_j)} \quad (13)$$

4. Final voting weights for staked liquidity W_t :

$$W_t = \frac{w_t}{\sum_{j=1}^{40} \left(\frac{1}{2} v_j + w_j \right)} \quad (14)$$

3.1.3 Liquid Carbon Yield

Defining:

- A : Total time-locked **A** tokens allocated for pricing of carbon classes, expressed as a proportion of the outstanding supply of **A** tokens.

With μ as the daily emission factor applied to the portfolio holding spot-delivery carbon:

$$\mu = \frac{A(1 - A)}{90} \quad (15)$$

Liquid Carbon Yield is allocated to time-locked **A** tokens holders using the (normalised) *initial voting weight* v_t determined in Equation 11.

3.2 Portfolio Manager

The Portfolio Manager's role of swapping **A** for carbon is managed through a set of smart contracts driven by allocation choices from the token system, the balances of assets held, and the discount rates generated by the Time-Locked Market.

The combined allocations of **A** and **G** tokens creates a dynamic pricing matrix by carbon class and by time, enabling spot and forward trading of carbon.

3.2.1 Purchase Carbon

*User swaps carbon credits for **A** tokens.*

3.2.1.1 Existing Carbon in the Portfolio

Carbon classes $i \in \{1, 2, 3, \dots, n\}$ are whitelisted through governance by time-locked **A** token and staked **AG** liquidity providers (see Section 3.1.2).

For carbon pricing, both **A** tokens and **G** tokens may be allocated to specific carbon classes i and these are independent allocations between the two-token systems.

For a carbon class quantity to be sold to the Automated Asset Manager, it must have a strictly positive quantity of **A** tokens allocated to that carbon class, otherwise there is no price, and the carbon cannot be sold.

Defining:

- C_i : Total tonnes of carbon class i currently held in the portfolio.
- A_i : **A** tokens allocated to carbon class i expressed as a proportion of the outstanding supply of **A** tokens, where $\sum A_i = A$.
- G_i : **G** tokens allocated to carbon class i expressed as a proportion of the outstanding supply of **G** Tokens.
- C_{it} : The quantity of carbon class i held in the Automated Asset Manager deliverable per maturity t where C_{i0} reflects the liquid quantity.

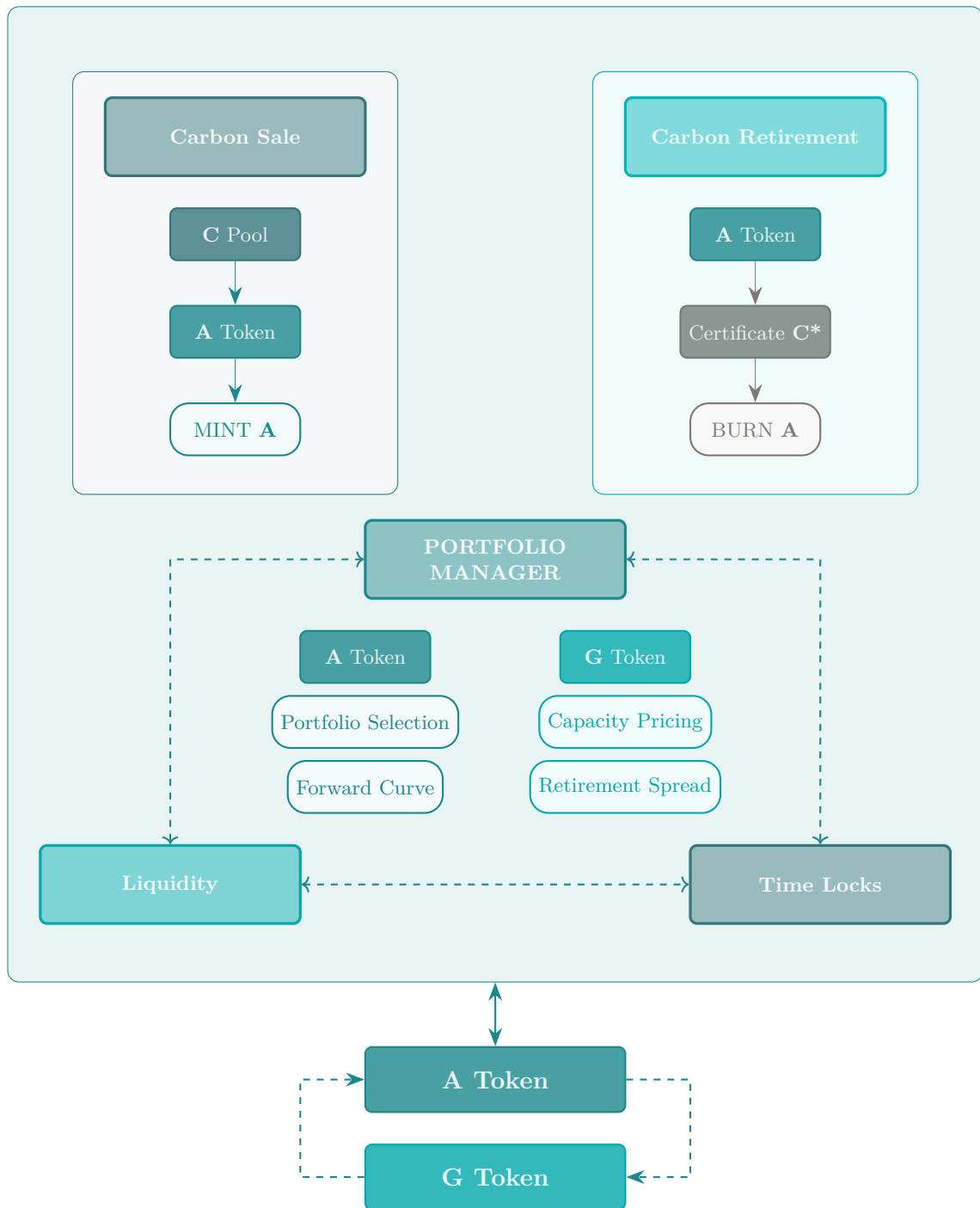


Figure 9: Klima 2.0 Portfolio Manager.

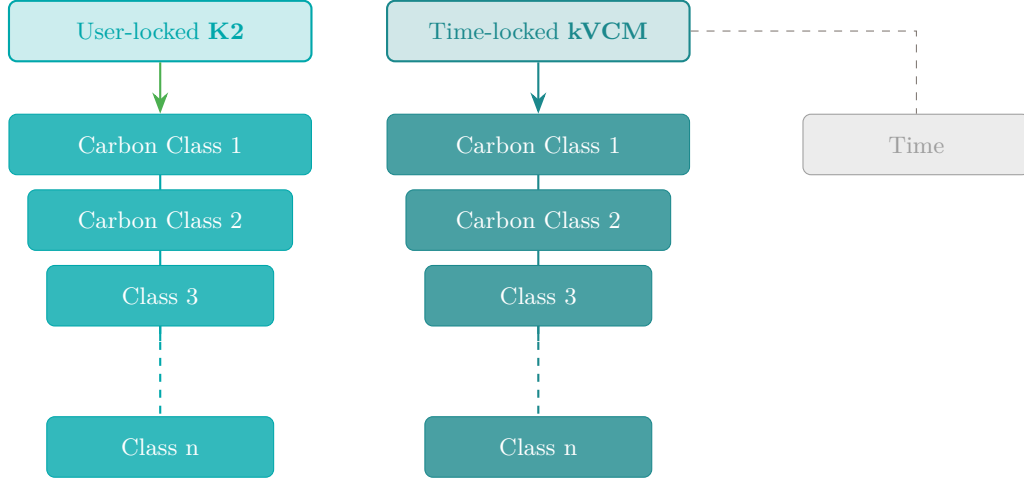


Figure 10: Token staking class structure.

In order to determine the present-value quantity of carbon, $\bar{C}_i$, we apply the discount curve from Equation 7 to the liquidity schedule and sum the discounted holdings:

$$\bar{C}_i = C_{i0} + \sum_{t=1}^{40} B_t C_{it} \quad (16)$$

Similarly, taking ΔC_{it} as the quantity of carbon i to be sold with a specific maturity index t :

$$\Delta \bar{C}_i = \Delta C_{i0} + \sum_{t=1}^{40} B_t \Delta C_{it} \quad (17)$$

Once standardised by the discount curve, trades can be aggregated in the same class for the defined trade or auction period.

Where $\Delta \bar{C}_i$ is expressed as the relative increment to its respective pool balance, the amount of **A** tokens issued to pay for carbon, ΔA , expressed as a proportion of current supply, is determined as:

$$\ln(1 + \Delta A) = \left(A_i - \frac{A_i^2 (1 - G_i)^2}{2} \right) \ln(1 + \Delta \bar{C}_i) \quad (18)$$

Denoting the expression on the right hand side of Equation 18 as RHS:

$$\Delta A = \exp(\text{RHS}) - 1 \quad (19)$$

Finally, ΔA is applied to the outstanding supply of **A** to solve for token quantities.

Figure 13 illustrates the **G** token's capacity to maintain the initial portfolio pricing of the **A** token. The data has been normalised in Figure 14 to $\Delta \bar{C}_i A_i$.

Noting that the sensitivity to G_i increases as A_i increases and the effects become more pronounced as $\Delta \bar{C}_i$ increases.

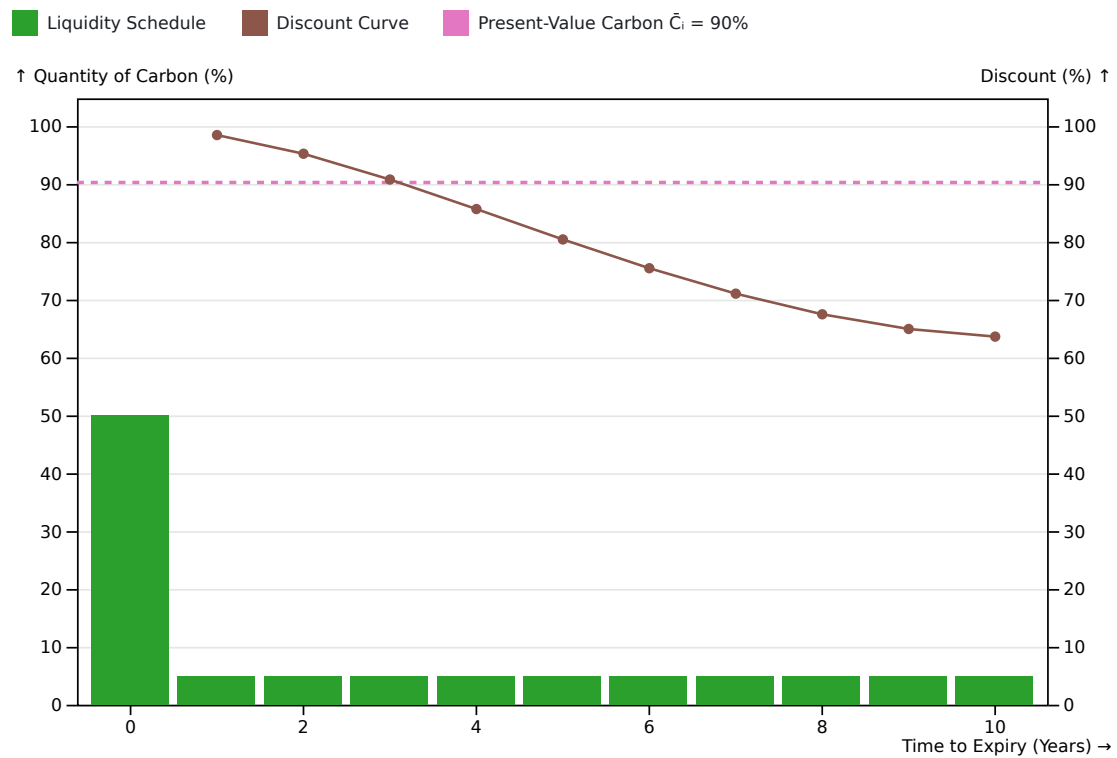


Figure 11: Carbon held in the portfolio.

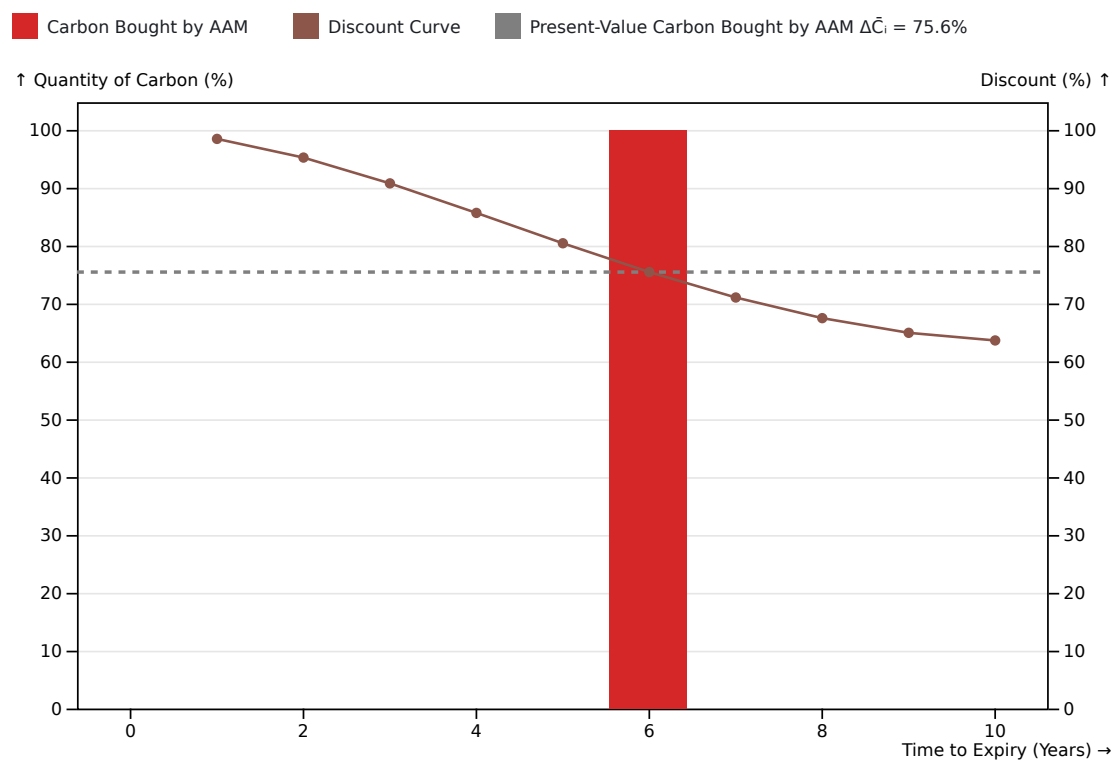


Figure 12: Carbon bought by the Portfolio Manager.

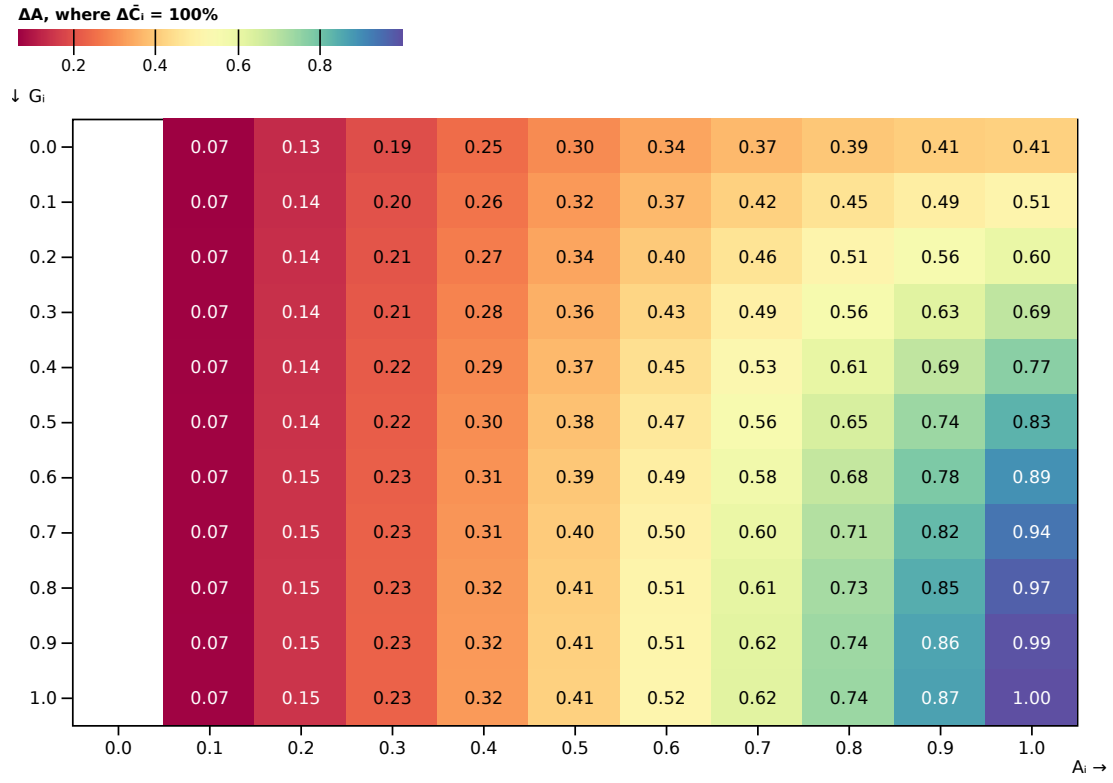


Figure 13: **A** price curves (ΔA).

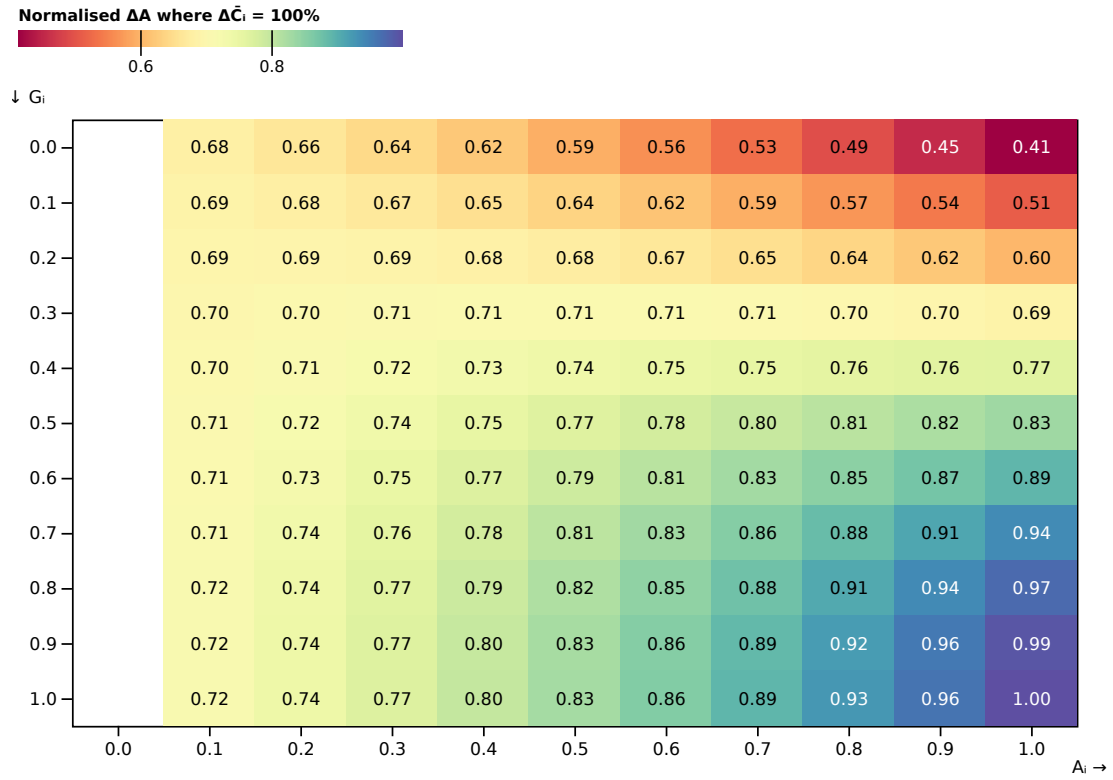


Figure 14: Normalised **A** price curves.

3.2.1.2 Zero Carbon Scenario

There are circumstances when there is zero carbon held in the portfolio for a particular class, i.e. $C_i = 0$, which invalidates the calculation of $\Delta\bar{C}_i$ and a different approach is required.

Taking $\Delta\bar{C}_\emptyset$ as the tonnes of carbon tokens (implying an existing balance of 1 tonne), adjusted for forward discounting, to be sold for any carbon class that has a strictly positive $\mathbf{A}$ allocation $A_\emptyset$, together with $\mathbf{G}$ allocation $G_\emptyset$:

$$\Delta A = \frac{\Delta\bar{C}_\emptyset}{1 + \Delta\bar{C}_\emptyset} \left(A_\emptyset - \frac{A_\emptyset^2(1 - G_\emptyset)^2}{2} \right)^2 \quad (20)$$

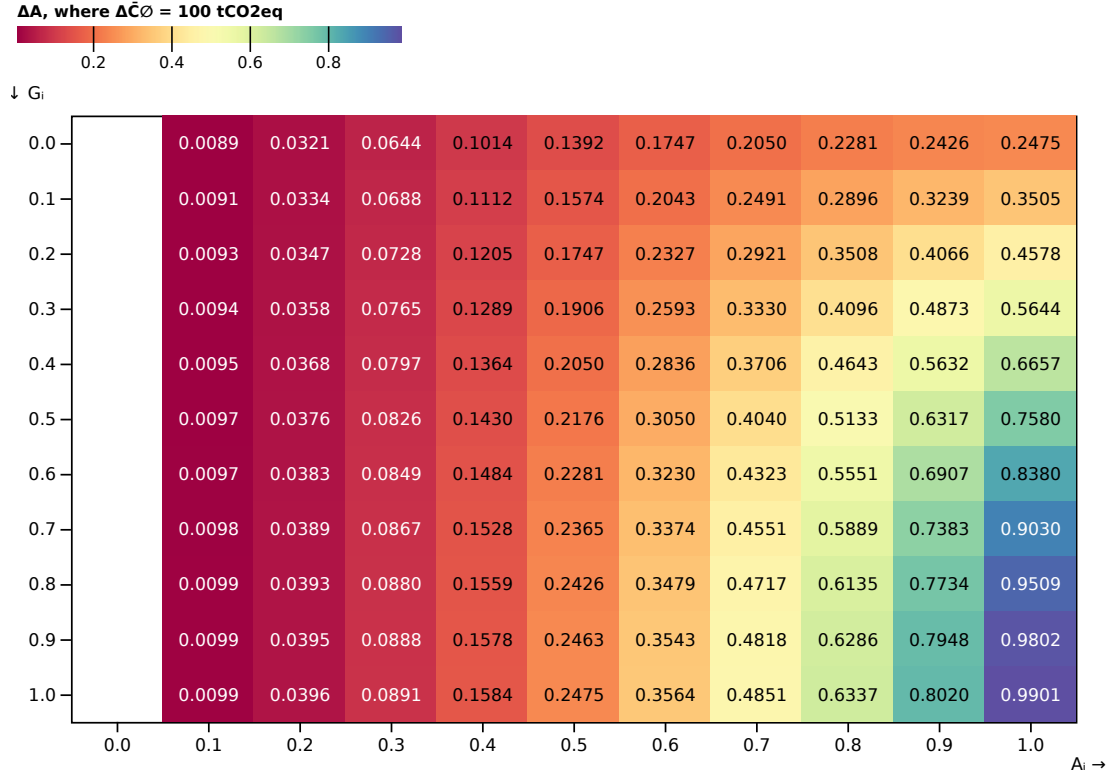


Figure 15: $\mathbf{A}$ price curves (ΔA) in the zero carbon scenario.

3.2.2 Sell Offset Certificates

User swaps $\mathbf{A}$ tokens for carbon offset certificates.

3.2.2.1 Weighted Carbon Class

For retiring carbon that is *weighted*, that is for which there is a strictly positive $\mathbf{A}$ token allocation, an $\mathbf{A}$ token holder can extract the carbon class offset certificate of their choice C_i but the available pool is only the liquid carbon balance, namely the element C_{i0} :

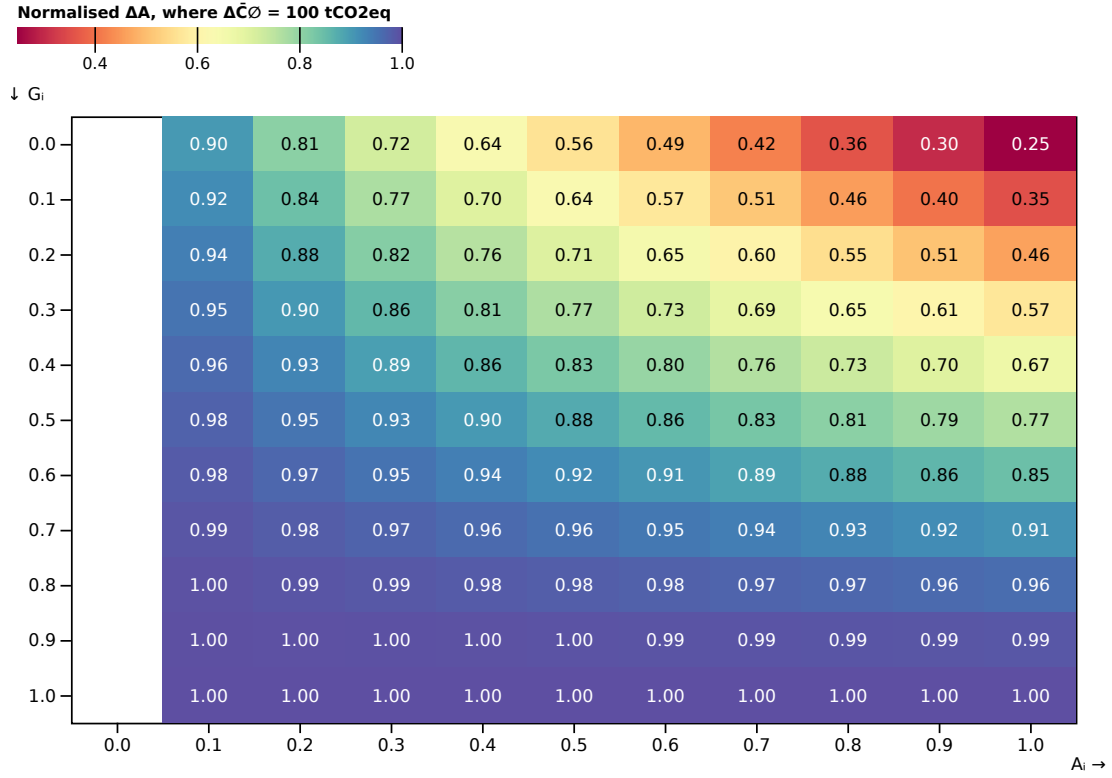


Figure 16: Normalised $\mathbf{A}$ price curves in the zero carbon scenario.

$$\ln(1 + \Delta C_i) = \frac{-\ln(1 + \Delta A)}{A_i + \frac{1}{2}A_i^2(1 - G_i)^2} \quad (21)$$

As before, denoting the expression on the right hand side of Equation 21 as RHS:

$$\Delta C_i = \exp(\text{RHS}) - 1 \quad (22)$$

Figure 17 shows the cost of carbon increasing with A_i and decreasing on G_i .

3.2.2.2 Unweighted Carbon Class

An offset certificate for a carbon class with a zero $\mathbf{A}$ allocation cannot be extracted from the portfolio by swapping in $\mathbf{A}$ tokens. However, it is still part of the Liquid Carbon Yield detailed in Section 3.1.3.

3.2.2.3 Liquidation: $\Delta A = 1$

In the event that 100% of $\mathbf{A}$ tokens are placed into the burn mechanism for carbon offset certificates, the balances of all carbon held in the portfolio post-trade are distributed to all $\mathbf{G}$ token holders.

Figure 18 below shows the spread captured on a ‘round trip’ by the system where ε is the proportion retained:

Figure 19 shows the component ‘spread’ contributions on a carbon sale and purchase round trip of a carbon offset certificate.



Figure 17: Proportion of carbon retired.

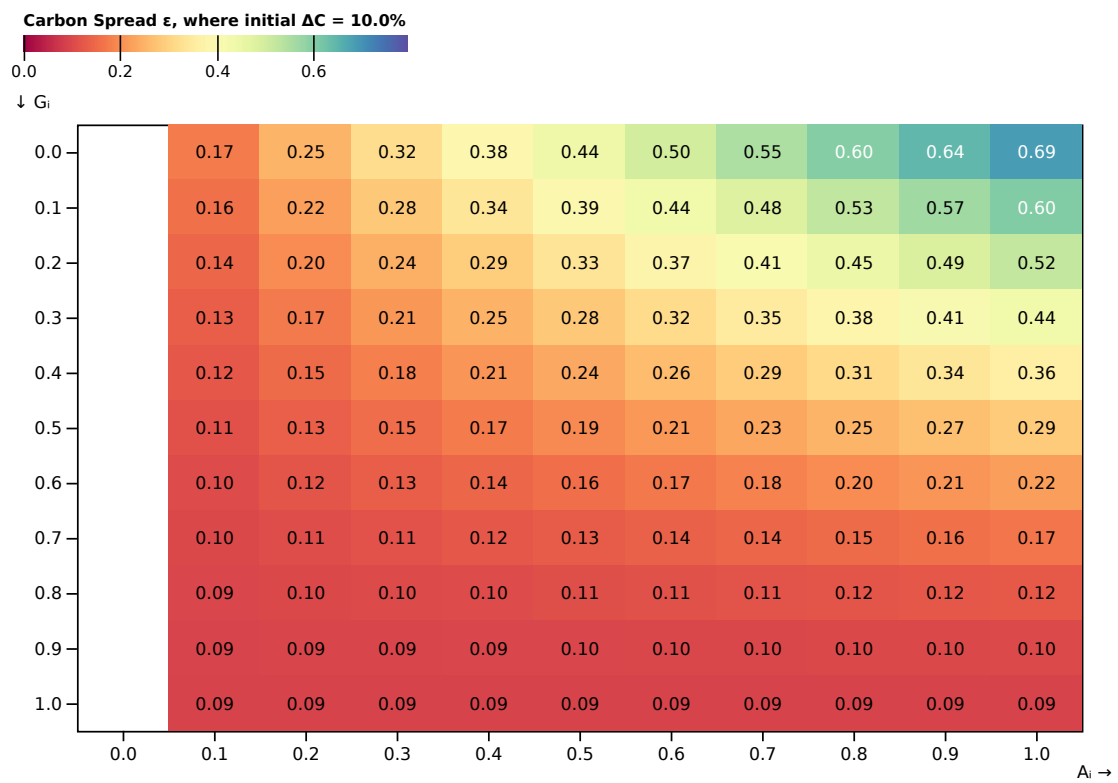
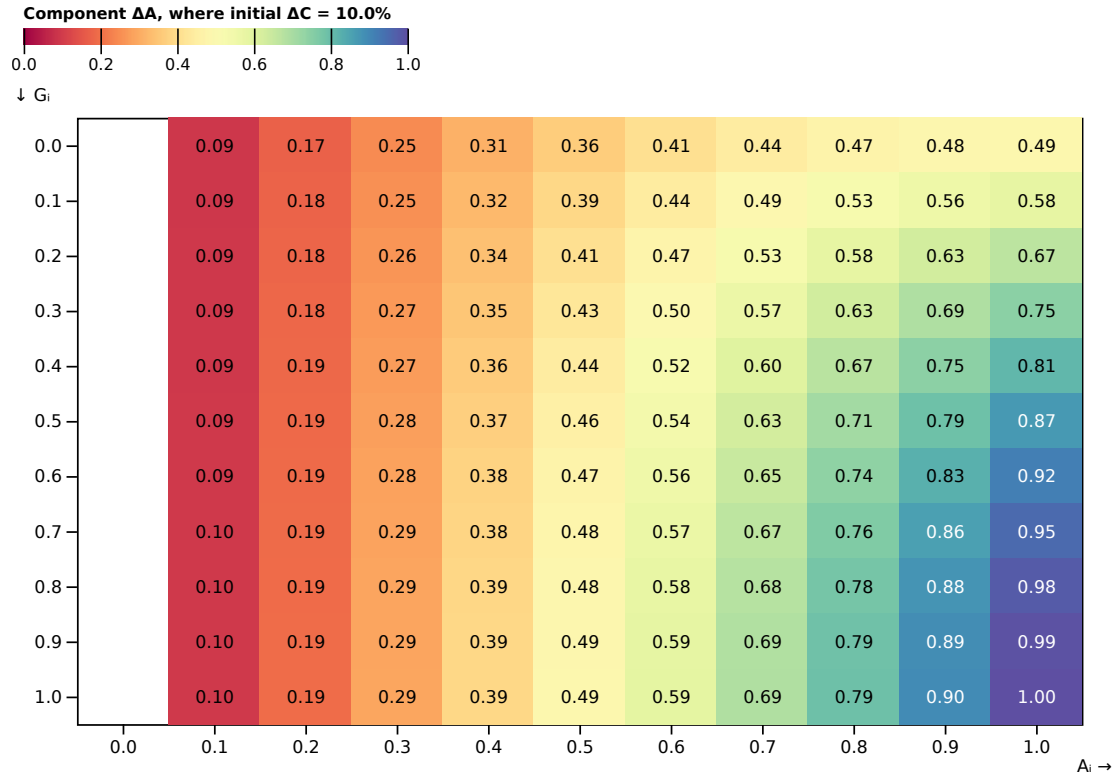
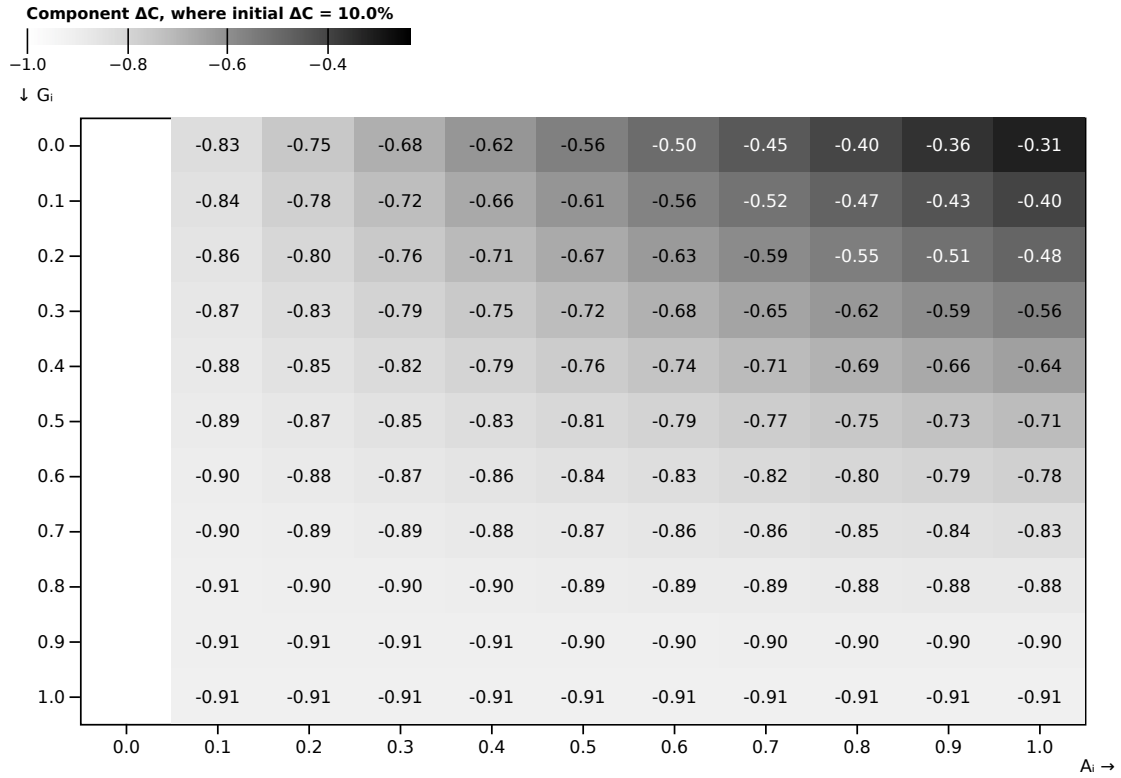


Figure 18: Carbon 'spread'.



(a) Carbon 'spread' component ΔA .



(b) Carbon 'spread' component ΔC .

Figure 19: Carbon 'spread' components.

3.3 Liquidity Markets

Both **A** and **G** tokens can be used for providing liquidity.

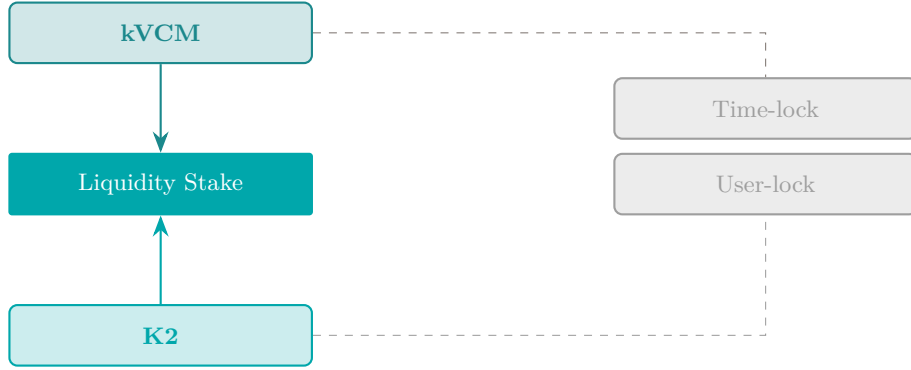


Figure 20: Token liquidity and pricing structure.

There are two core liquidity pools:

1. An AAM 50:50 pairing of **A** and **G** tokens: pool $\overline{\mathbf{AG}}$.
2. A hard currency USDC denoted as **Q** paired with **A**: pool $\overline{\mathbf{AQ}}$.

3.3.1 Liquidity Fees

The $\overline{\mathbf{AQ}}$ pool will have its own set of fees in the normal way.¹

The $\overline{\mathbf{AG}}$ pool has different economics as the assets are highly correlated since they represent the same economy. For this reason, the fees are extremely low.

By staking liquidity (liquidity provider tokens) to the **standard maturities**, both pools may receive a distribution of **A** tokens determined from the Risk Premium calculation below. This is an additional primary issuance to the Base Accrual already discussed.

3.3.2 Risk Premium: Beta Determination

We can consider the Time-Locked Market yield as the system's *risk-free* rate. In addition to this mechanism, a *risky* spread is determined that is ultimately paid to the staked liquidity providers of the **A** and **G** tokens as compensation for the risk levels assumed.

As we have seen, the **G** token has an impact on risk-pricing of **A**. As **G** staking increases, the relationship between the carbon class selected under G_i and the portfolio token **A** strengthens. We can consider G_i staking as an estimate of residual or idiosyncratic risk in the carbon class and this allows us to calculate a portfolio beta β from the implied betas of each carbon class i .

$$\beta = \sqrt{\sum_{i=1}^n A_i - A_i (1 - G_i)^2} \quad (23)$$

¹Note the development of liquidity pool pricing functionality may be applicable.

The portfolio β determines a yield factor for the liquidity pools of $\mathbf{A}$ to compensate for the implied risk levels.

For intuition, the map in Figure 21 shows the various outputs of the function per carbon class.

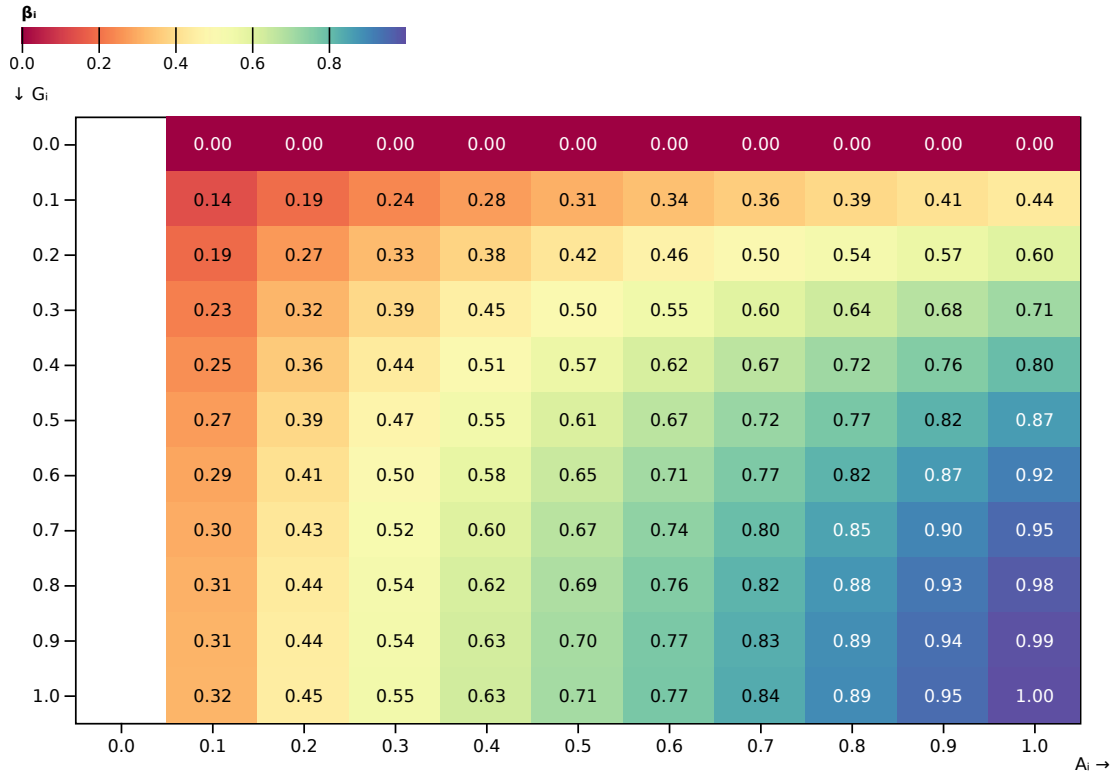


Figure 21: Range of β_i .

The table and figure below show an example of the effects on β of allocating large G_i values to small A_i values where the shift in G_i results in a lower β (0.27 from 0.55) with no change to total $\mathbf{G}$ and $\mathbf{A}$ allocations.

Class	1	2	3	4	β
A_i	0.50	0.20	0.10	0.05	
Initial G_i	0.30	0.10	0.05	0.01	
Initial β_i^2	0.2550	0.0380	0.0098	0.0010	0.5511
New G_i	0.01	0.05	0.10	0.30	
New β_i^2	0.0100	0.0195	0.0190	0.0255	0.2719
ΔG_i	(0.29)	(0.05)	0.05	0.29	
$\Delta \beta_i^2$	(0.2451)	(0.0185)	0.0092	0.0245	

Table 2: Effect on β from outsized $\mathbf{G}$ allocation.

Figure 22 shows β 's sensitivity to $\mathbf{G}$ allocation as a function of $\mathbf{A}$ allocation; that is to say that a large G_i stake on a small A_i stake has limited effects (notwithstanding other consequential factors).

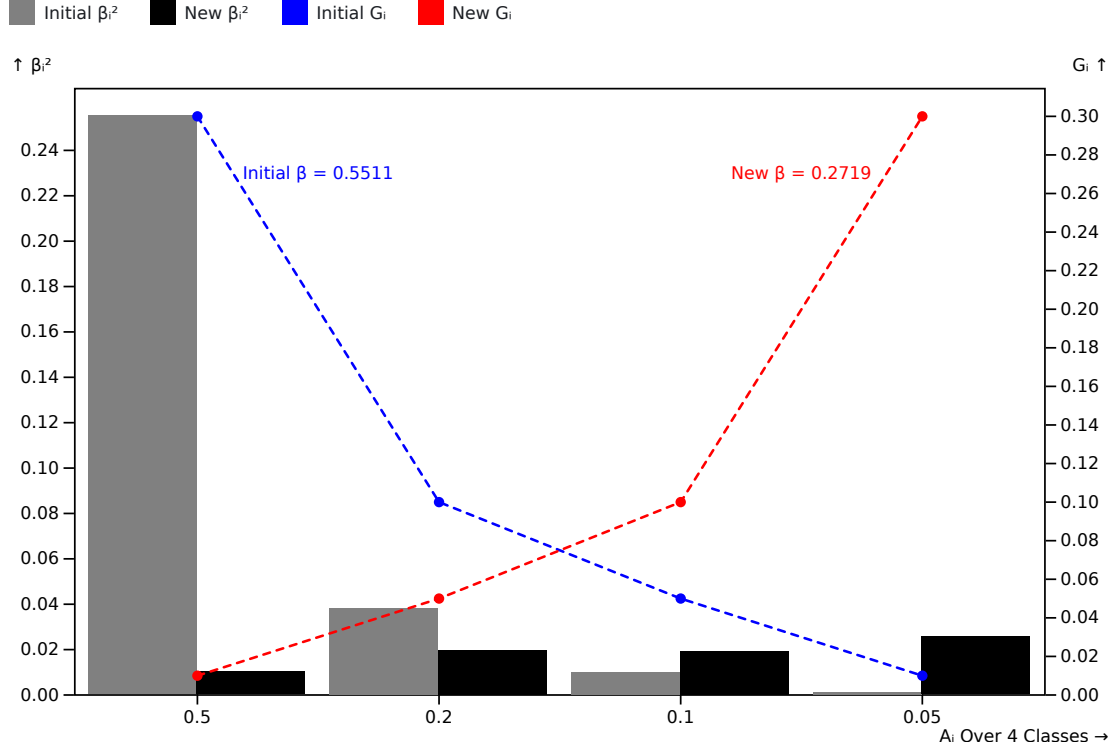


Figure 22: Example of $\mathbf{G}$ allocation on β .

3.3.3 Allocation of Risk Premium

The full issuance of $\mathbf{A}$ tokens is depicted below including now the Risk Premium for the liquidity pools accordingly.

3.3.4 Share of Risk Premium

The Risk Premium allocation is shared between user-locked $\mathbf{G}$ tokens, $\overline{\mathbf{AG}}$, and $\overline{\mathbf{AQ}}$ pools, with shares λ_{GG} , λ_G , and λ_Q respectively.

Defining:

- G_G : Total $\mathbf{G}$ tokens in the $\overline{\mathbf{AG}}$ pool, expressed as a proportion of the outstanding supply of $\mathbf{G}$.
- A_G : Total $\mathbf{A}$ tokens in the $\overline{\mathbf{AG}}$ pool, expressed as a proportion of the outstanding supply of $\mathbf{A}$.
- A_Q : Total $\mathbf{A}$ tokens in the $\overline{\mathbf{AQ}}$ pool, expressed as a proportion of the outstanding supply of $\mathbf{A}$.

The allocation to user-locked $\mathbf{G}$ tokens, λ_{GG} :

$$\lambda_{GG} = \frac{1 - A_Q}{1 + \left(\frac{\sum_{i=1}^n G_i}{G_G} \right)^2} \quad (24)$$

Noting the relationship between G and β , and particularly if $G = 0$, $\beta = 0$.

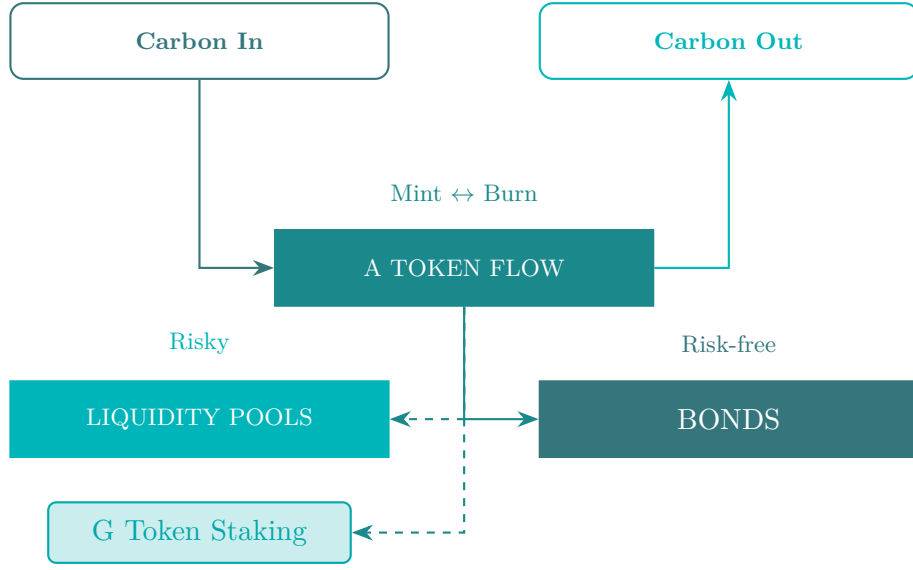


Figure 23: **A** token flow structure.

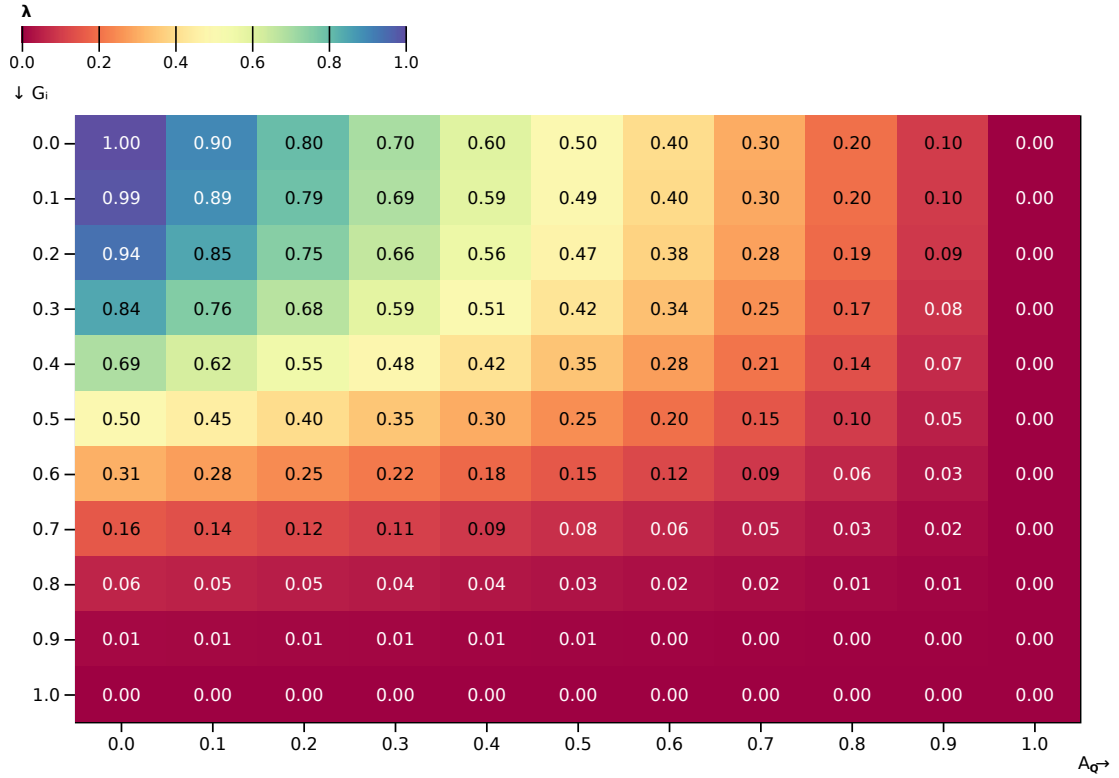


Figure 24: **G** stake allocation (assuming $G_G = 1 - G_i$).

The residual share, $1 - \lambda_{GG}$, is split between the liquidity pools:

$$\lambda_G = (1 - \lambda_{GG}) \frac{2A_G}{2A_G + A_Q\sqrt{2}} \quad (25)$$

For completeness:

$$\lambda_Q = 1 - \lambda_{GG} - \lambda_G \quad (26)$$

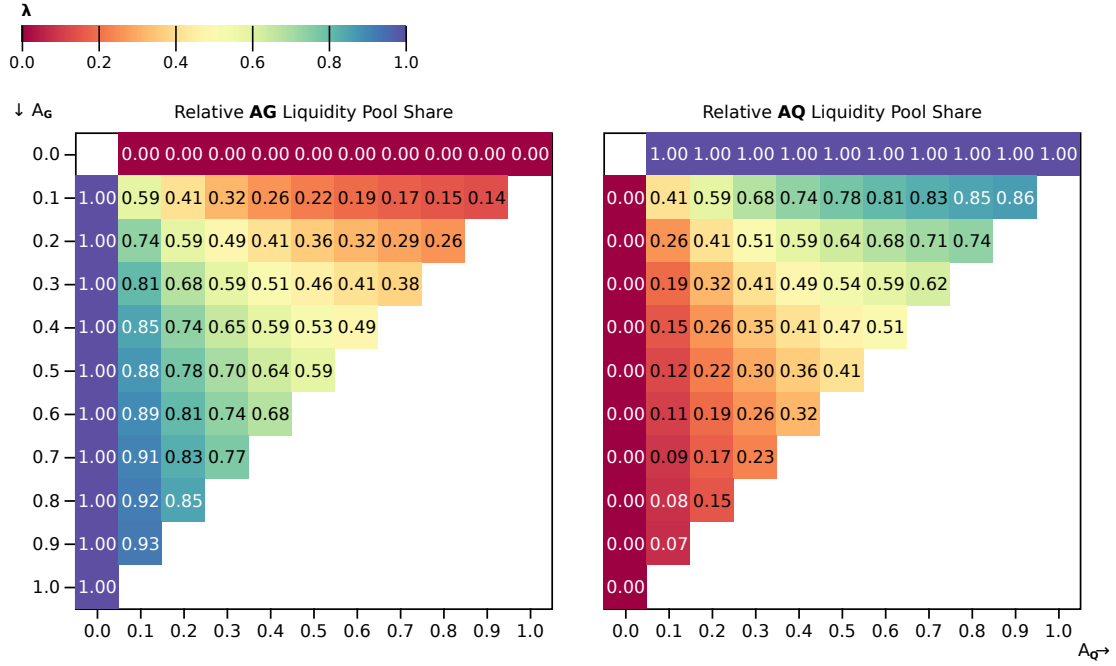


Figure 25: Liquidity pool split λ_G, λ_Q .

3.3.5 Risk Premium Distribution

For $\lambda_{GG}, \lambda_G, \lambda_Q$ we apply β :

$$\Lambda_X = \lambda_X \beta, \quad \text{for } X \in \{GG, G, Q\} \quad (27)$$

Taking b as a discount parameter:

$$b = \frac{\sum_{t=1}^{40} Z_t S_t B_t}{\sum_{t=1}^{40} Z_t S_t} \quad (28)$$

The total Risk Premium tokens R_λ :

$$R_\lambda = b R (\Lambda_{GG} + \Lambda_G + \Lambda_Q) \quad (29)$$

The allocations of R_λ are pro-rata to $\Lambda_{GG}, \Lambda_G, \Lambda_Q$, and thereafter:

1. Locked $\mathbf{G}$: Λ_{GG} in proportion to $\mathbf{G}$.
2. Locked $\overline{\mathbf{AG}}$, $\overline{\mathbf{AQ}}$ tokens are allocated a weighting G_t , Q_t depending on their time bucket t :

$$G_t = \frac{Z_t L_{Gt} B_t}{\sum Z_t L_{Gt} B_t} \quad (30)$$

$$Q_t = \frac{Z_t L_{Qt} B_t}{\sum Z_t L_{Qt} B_t} \quad (31)$$

Where L_{Gt} , L_{Qt} are the proportion of all liquidity locked in each time bucket for $\overline{\mathbf{AG}}$ and $\overline{\mathbf{AQ}}$ respectively.

Thereafter each time bucket allocation is proportionate to staked liquidity provider token holdings.

4 Klima 2.0 Token Distribution

4.1 Planned Allocations

Cohort	Proportion	Quantity (m)
Klima Holders	87.5%	17.5
DAO/Treasury	10.0%	2.0
01X	2.5%	0.5
Total	100.0%	20.0

Table 3: **kVCM** token.

Cohort	Proportion	Quantity (m)	Liquidity
Klima Holders	40.0%	40.0	Logistic Vesting 48 months
Ecosystem Grant	5.0%	5.0	Logistic Vesting 48 months
Programmatic Incentives	40.0%	40.0	Incentive Curve
pKlima Holders	3.0%	3.0	Logistic Vesting 48 months
DAO/Treasury	4.5%	4.5	24 month locked LP of $\overline{\mathbf{AG}}$
01X	2.5%	2.5	24 month locked LP of $\overline{\mathbf{AG}}$
Product Design and Development	5.0%	5.0	Logistic Vesting 48 months
Total	100.0%	100.0	

Table 4: **K2** token.

■ Incentives ■ Klima Holders ■ Product Design ■ Ecosystem Grant ■ DAO/Treasury ■ pKlima Holders

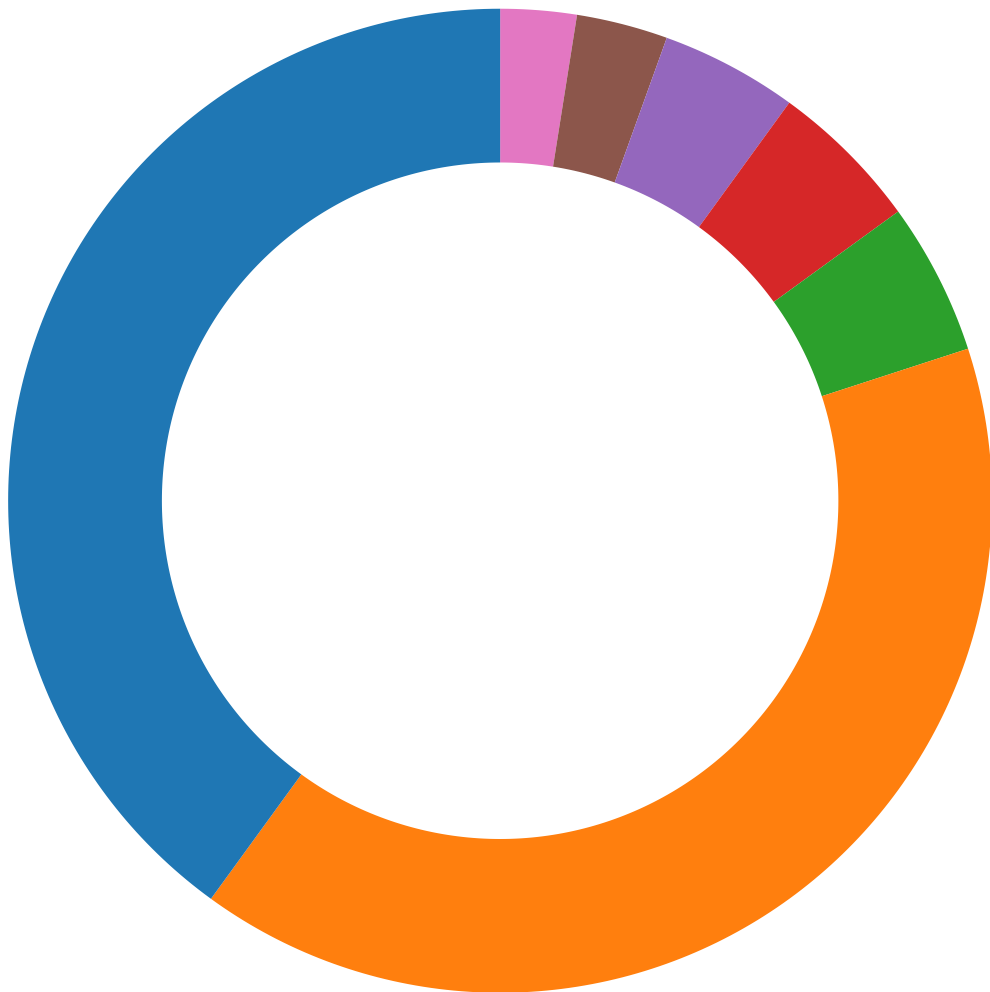


Figure 26: **K2** token allocations.

4.2 Programmatic Incentive Curve

The incentive issuance is built on a logistic function, P , to generate total proportion of supply in issue. It is calibrated from the initial issuance at TGE P_0 and the inflection point time T where 50% of $\mathbf{G}$ token incentives have been released.

Setting x_0 from the initial supply parameter:

$$x_0 = \ln \left(\frac{P_0}{1 - P_0} \right) \quad (32)$$

With x_t at time point $t \in (0, \infty)$:

$$x_t = x_0 \left(1 - \frac{t}{T} \right) \quad (33)$$

Giving supply function $P(t)$ as:

$$P(t) = \frac{\exp(x_t)}{\exp(x_t) + 1} \quad (34)$$

P_0 set at 7% and T at 24 months:

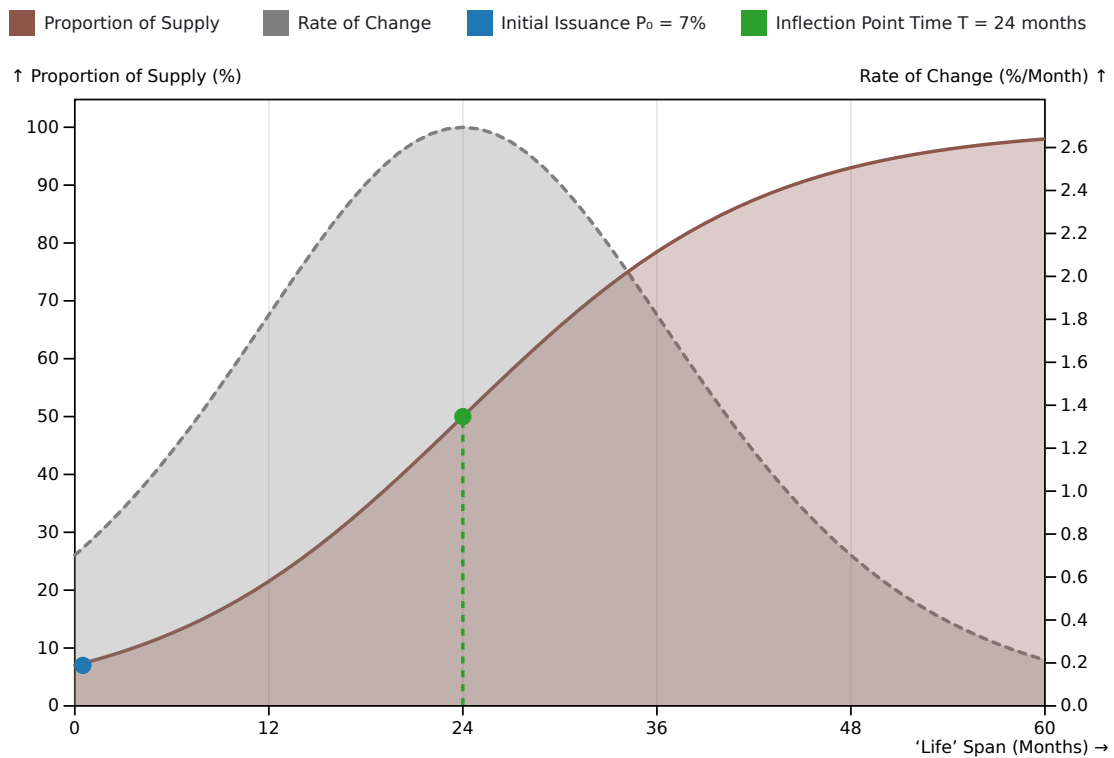


Figure 27: Incentive Issuance

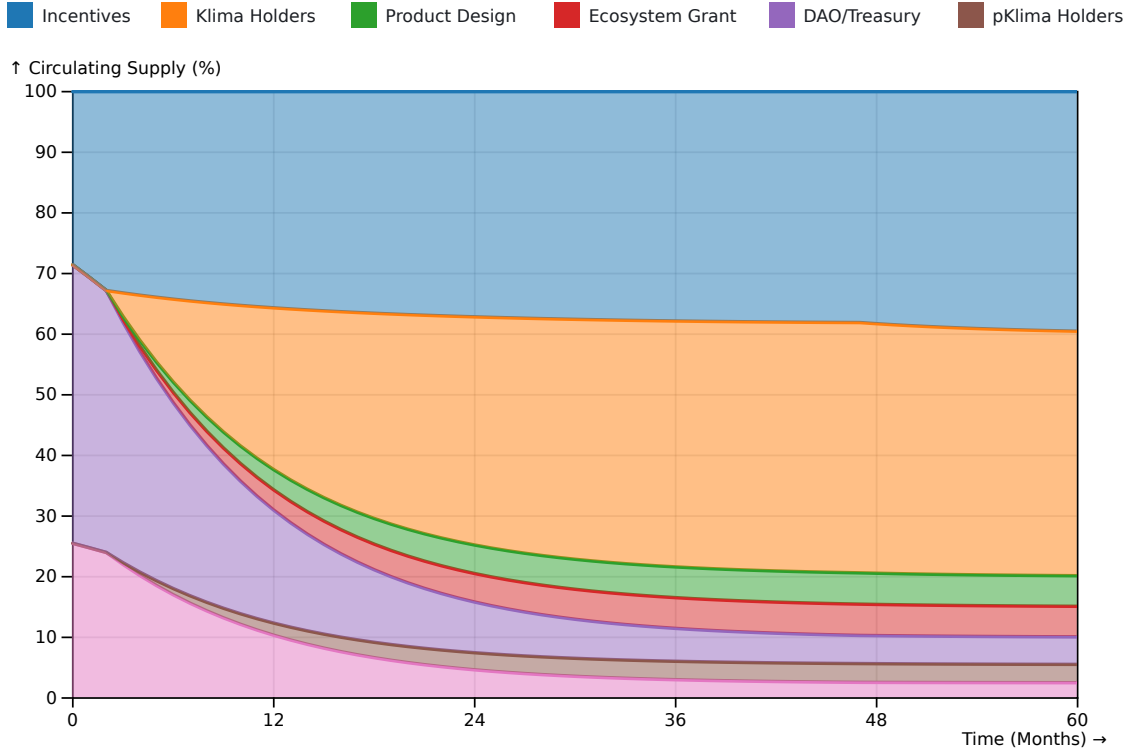


Figure 28: **K2** token circulating supply over time.

4.3 Incentive Allocations

The **relative utilisation** measurement factor v is calculated as follows.

Defining initially:

- G : Total **G** tokens staked expressed as a proportion of the circulating supply, $G \in [0, 1]$.
- L : Total **G** tokens held in the **AG** pool expressed as a proportion of circulating supply, $L \in (0, 1]$.

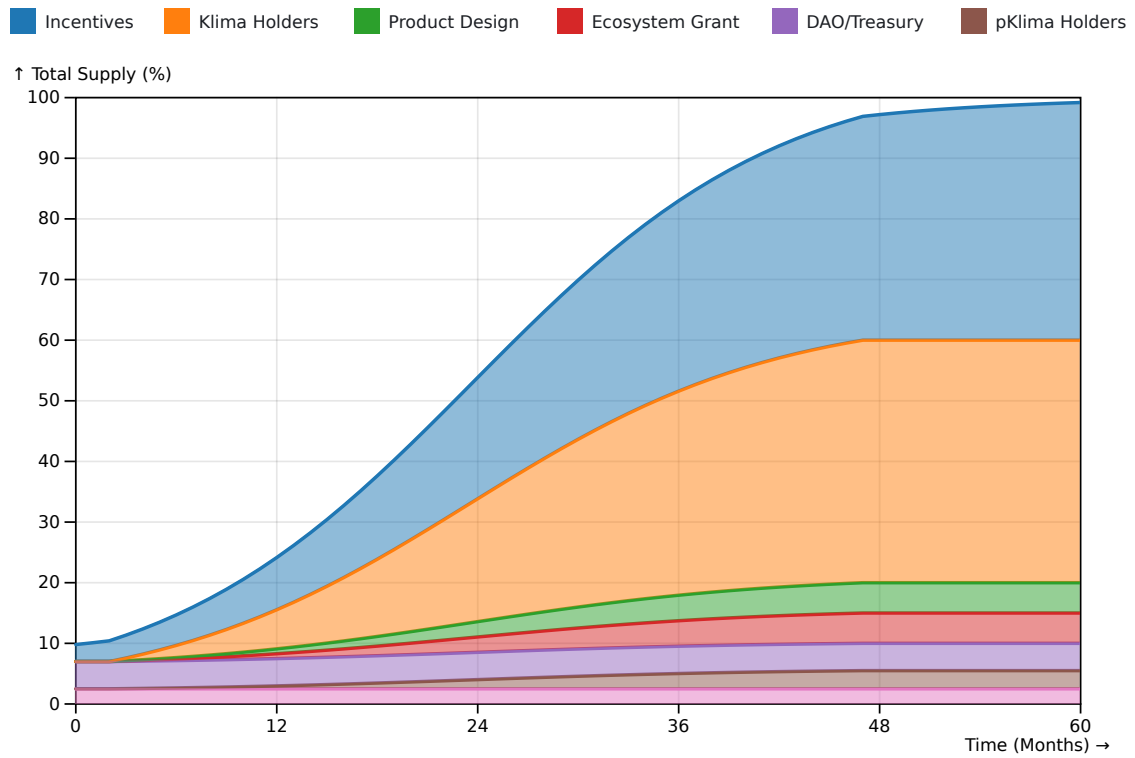
Where $v = 0$ if $G + L = 0$, otherwise:

$$v = \left(\frac{2GL}{G^2 + L^2} \right)^2 \quad (35)$$

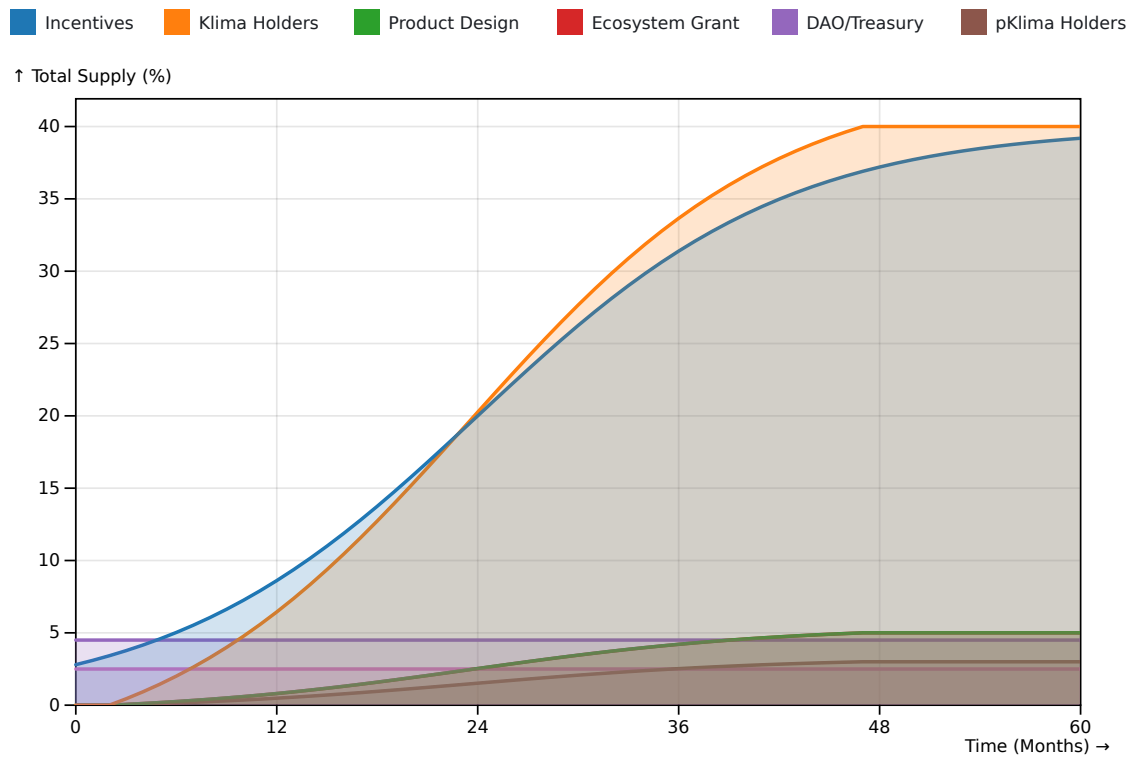
The **absolute utilisation** parameter η is defined as $\eta = 0$ if $G + L = 0$, otherwise:

$$\eta = \frac{2GL}{G(1 - G) + L(1 - L)} \quad (36)$$

Incentives I are allocated as follows:

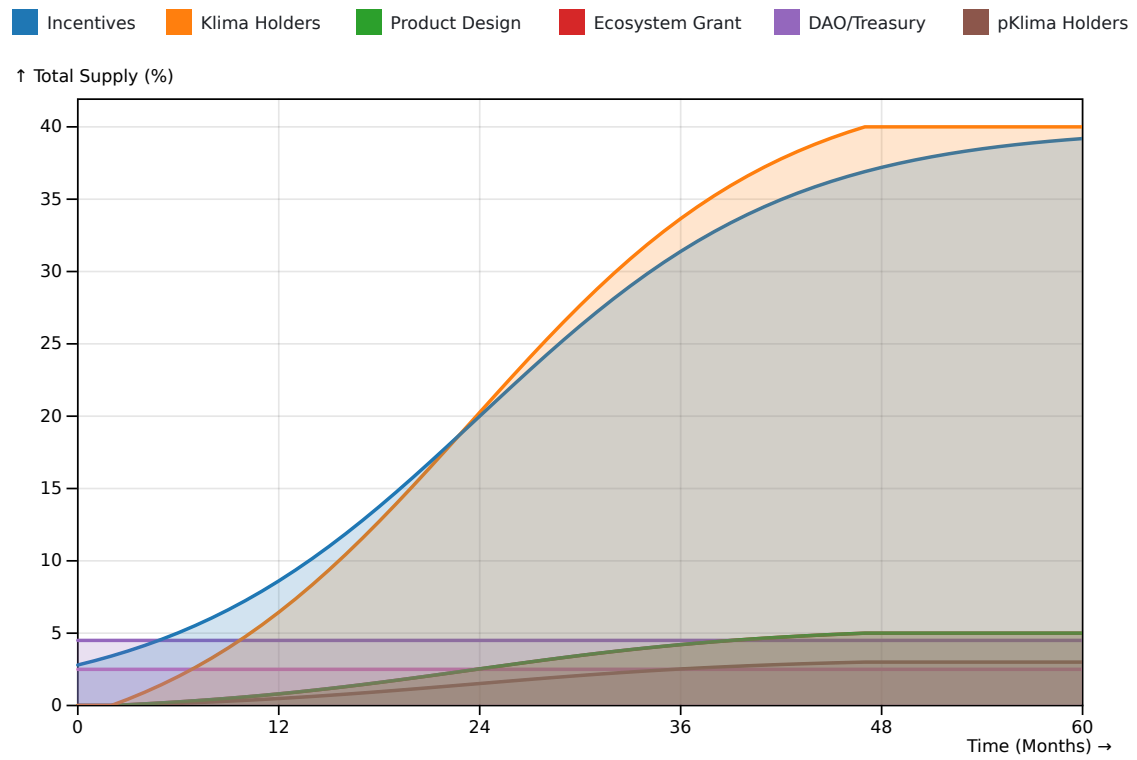


(a) Total supply (stacked).

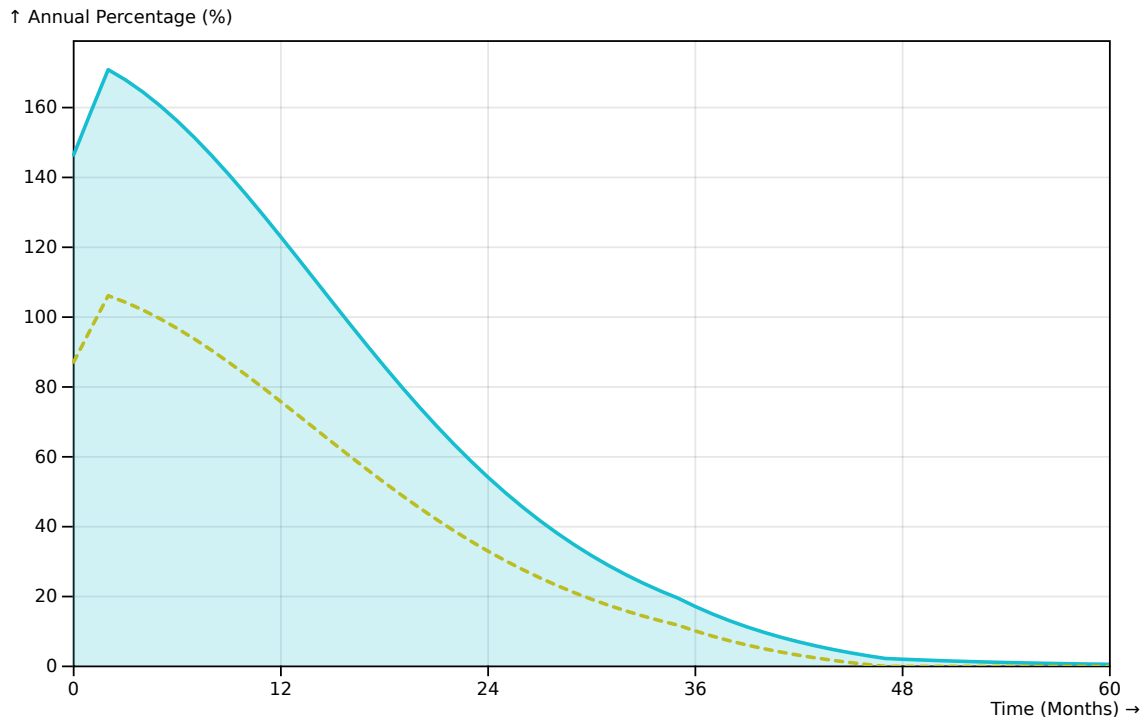


(b) Total supply (unstacked).

Figure 29: **K2** token total supply over time.



(a) Total supply differential (stacked).



(b) Utility incentive yield.

Figure 30: **K2** token supply risk metrics.

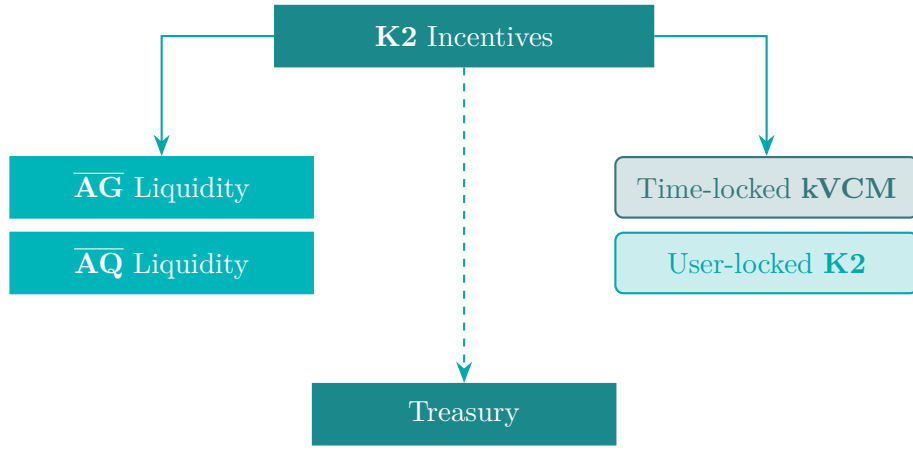


Figure 31: **K2** token incentive distribution structure.

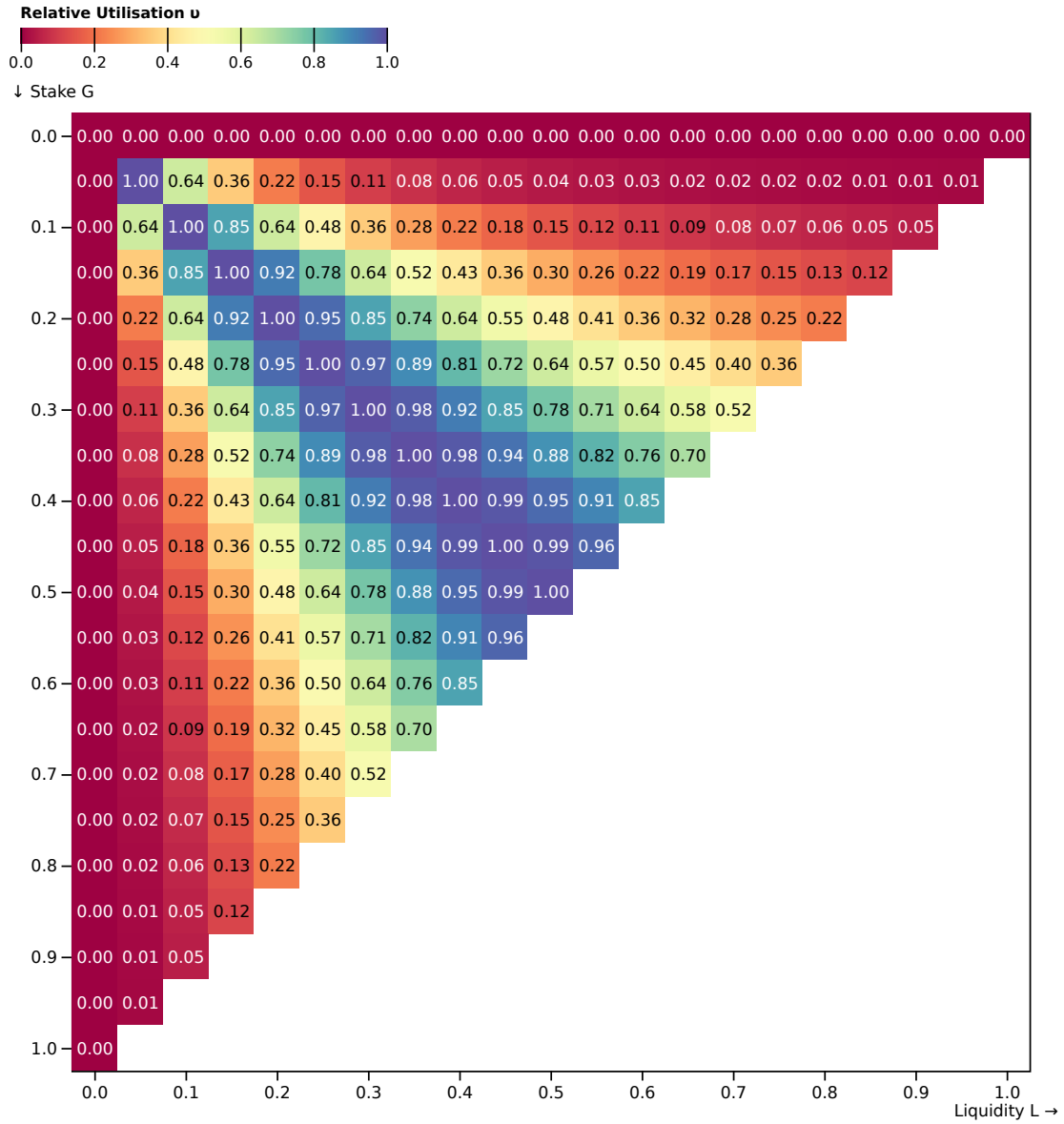


Figure 32: Upsilon v range of values.

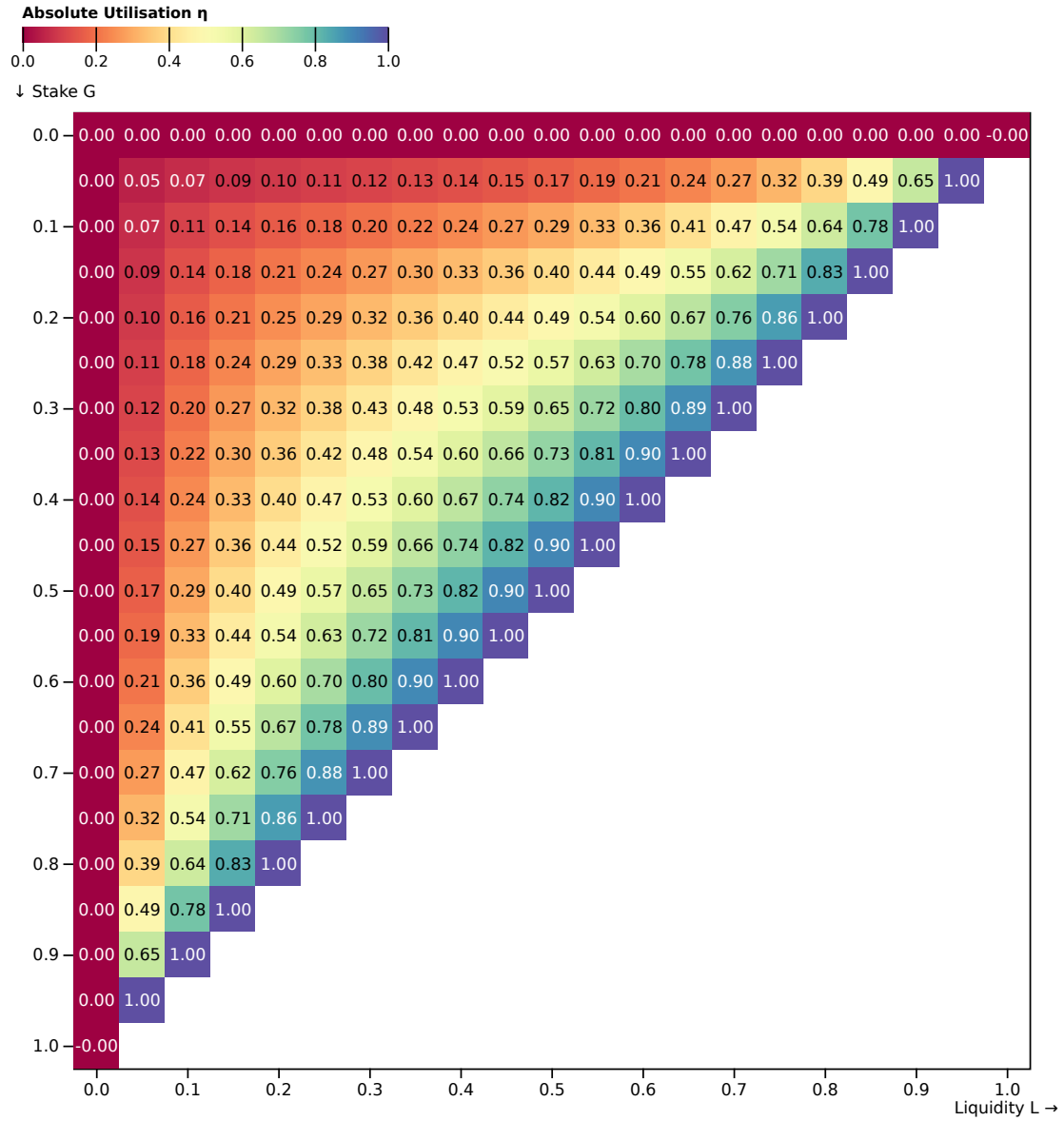


Figure 33: Eta η range of values.

4.3.1 Treasury

The allocation to the Treasury I_T is the imbalance generated from v :

$$I_T = 1 - v \eta \quad (37)$$

4.3.2 Post Treasury

The residual post-treasury allocation is shared four ways within 2 buckets:

1. Time-locked **A** & user-locked **G** tokens

Where S is the proportion of time-locked **A** tokens (as defined previously in Section 3.1):

1. Time-locked **A**, I_S :

$$I_S = S \frac{L^2}{G^2 + L^2} \quad (38)$$

2. User-locked **G**, I_G :

$$I_G = (1 - S) \frac{L^2}{G^2 + L^2} \quad (39)$$

2. Liquidity

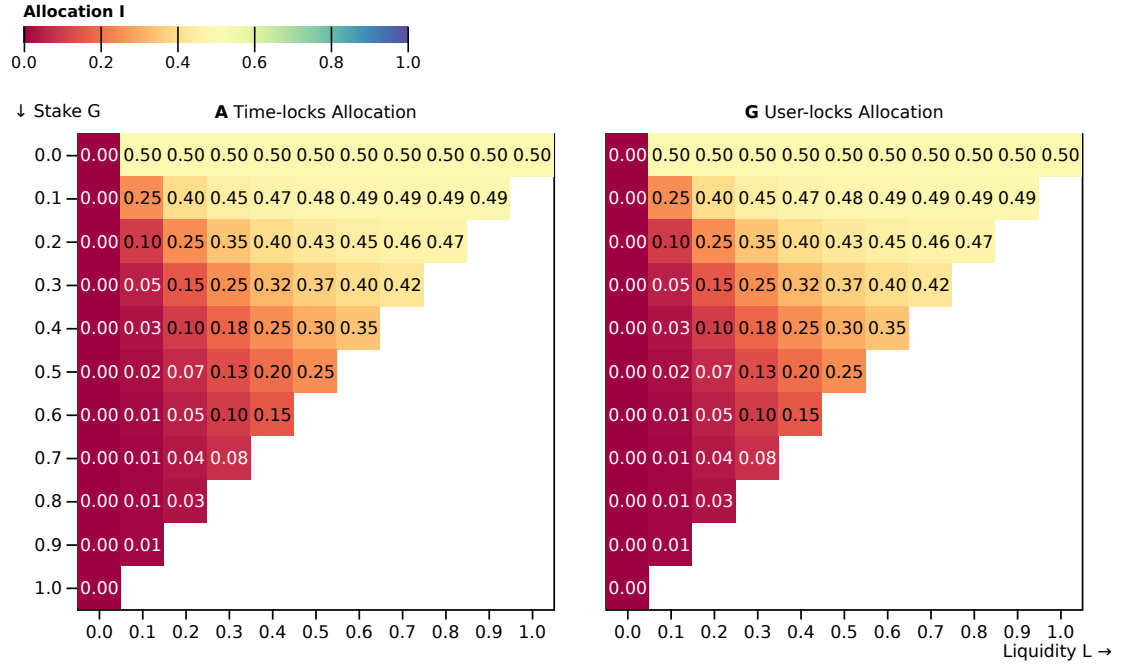
With λ_G , λ_Q , λ_{GG} as defined in Section 3.3.4:

3. $\overline{\mathbf{AG}}$ pool I_{AG} :

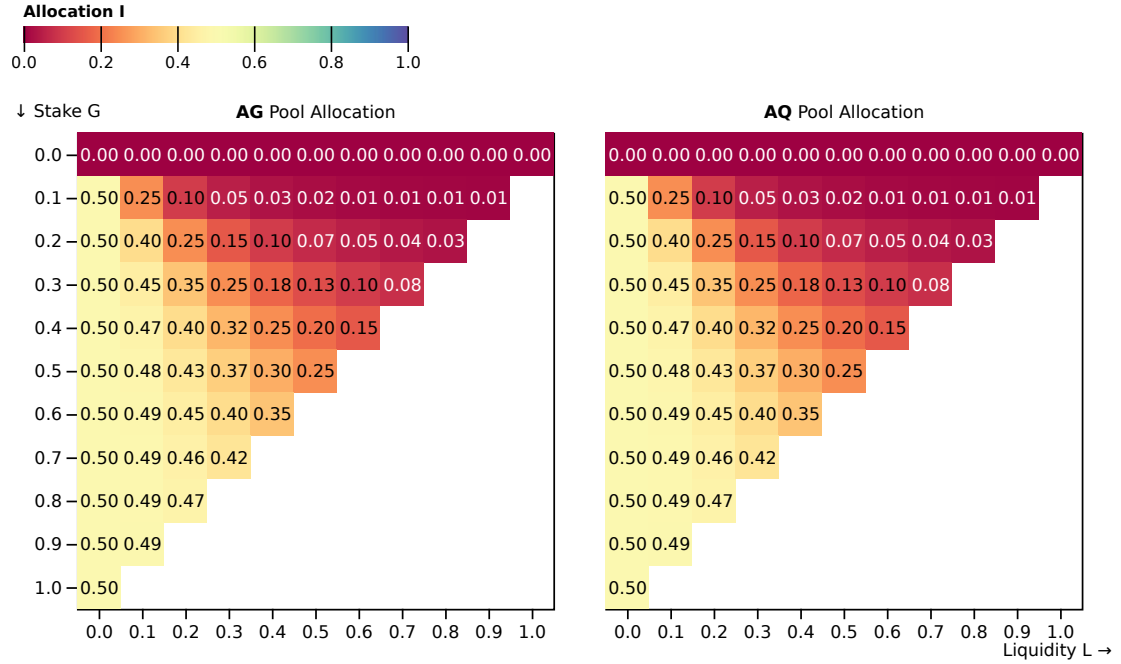
$$I_{AG} = \frac{\lambda_G}{1 - \lambda_{GG}} \frac{G^2}{G^2 + L^2} \quad (40)$$

4. $\overline{\mathbf{AQ}}$ pool I_{AQ} :

$$I_{AQ} = \frac{\lambda_Q}{1 - \lambda_{GG}} \frac{G^2}{G^2 + L^2} \quad (41)$$



(a) Time-locked **A** and user-locked **G** allocations.



(b) Liquidity pools allocations

Figure 34: Share of non-treasury incentives I_S , I_G , I_{AG} and I_{AQ} .

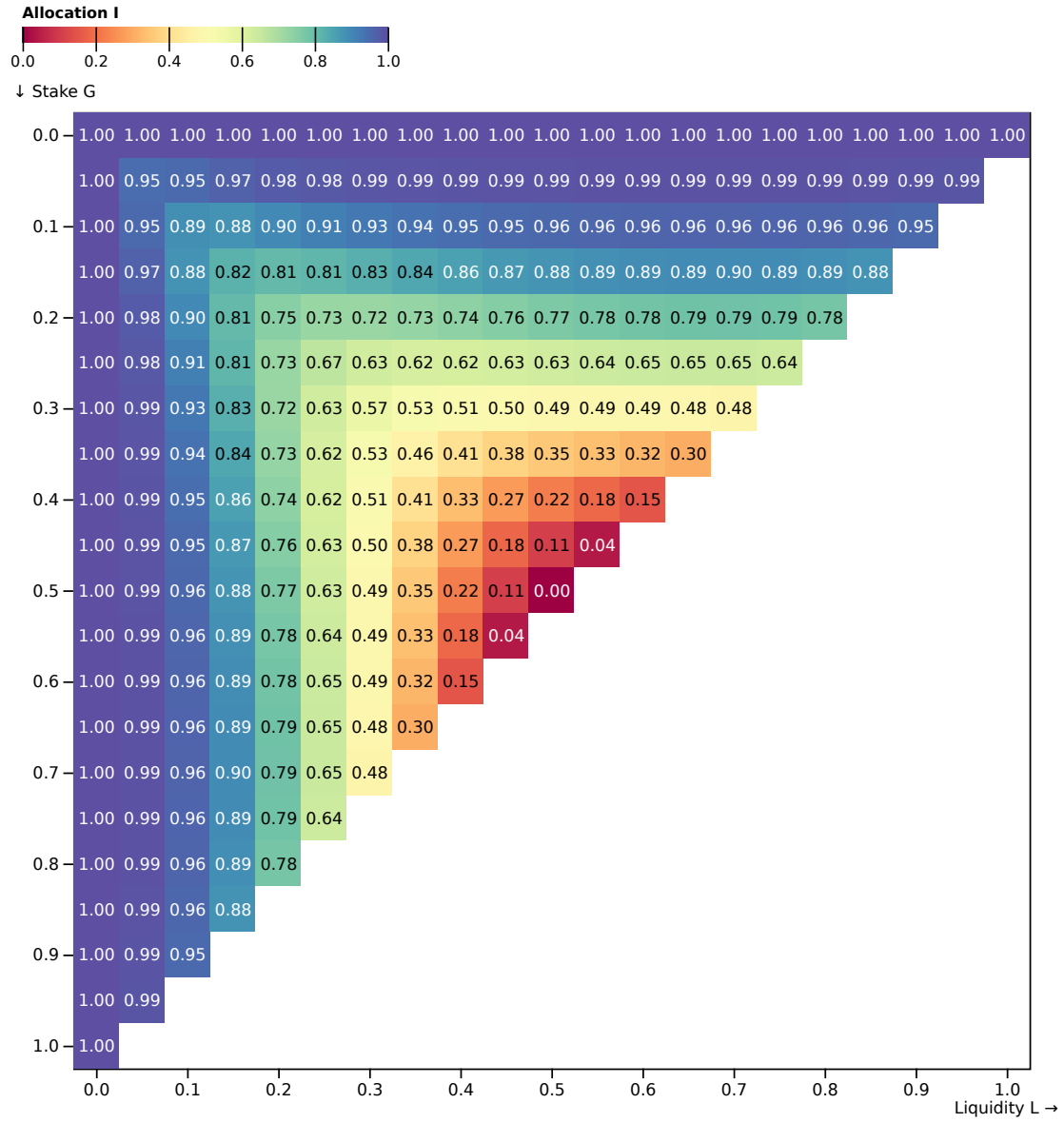


Figure 35: Treasury incentives I_T .